

2.2

GIVEN: CARBON DIOXIDE AT

$$p = 300 \frac{\text{kN}}{\text{m}^2} \text{ ABSOLUTE AND } T = 60^\circ\text{C}$$

FIND: DENSITY AND SPECIFIC WEIGHT

SOLUTION: OBTAIN CO_2 DENSITY BY APPLYING THE IDEAL GAS LAW.

$$\rho = \frac{p}{RT}$$

OBTAIN GAS CONSTANT, R , FROM TABLE A.2

$$R = 189 \frac{\text{J}}{\text{kg}\cdot\text{K}} \quad 1 \text{ J} = 1 \text{ N}\cdot\text{m}$$

$$\rho = \frac{300,000 \frac{\text{N}}{\text{m}^2}}{\left(189 \frac{\text{N}\cdot\text{m}}{\text{kg}\cdot\text{K}}\right)(333 \text{ K})} = 4.77 \frac{\text{kg}}{\text{m}^3}$$

$$\rho = 4.77 \frac{\text{kg}}{\text{m}^3}$$

SPECIFIC WEIGHT

$$\gamma = \rho g$$

$$\gamma = 46.7 \frac{\text{N}}{\text{m}^3}$$

2.5 GIVEN: AIR AND WATER AT $T = 100^\circ\text{C}$
AND $P = 5$ ATMOSPHERES

FIND: DENSITY RATIO, ρ_w/ρ_a

SOLUTION:

WATER — ASSUME THAT THE WATER
IS INCOMPRESSIBLE AND USE
TABLE A.5 TO OBTAIN ρ_w

$$\rho_w = 958 \frac{\text{kg}}{\text{m}^3}$$

AIR — USE IDEAL GAS LAW
TO CALCULATE ρ_a .

$$\rho_a = \frac{p_a}{R T_a} \quad p_a = 5 \left(101,000 \frac{\text{N}}{\text{m}^2} \right)$$

$$T_a = 100 + 273 = 373 \text{ K}$$

$$\rho_a = \frac{505,000}{(287)(373)} = 4.72 \frac{\text{kg}}{\text{m}^3}$$

$$\frac{\rho_w}{\rho_a} = 203 \quad \text{DIMENSIONLESS}$$

2.13

GIVEN: WATER AND AIR AT STANDARD
ATMOSPHERIC PRESSURE, $p = 101 \text{ kN/m}^2$.

FIND: CHANGE IN ρ AND μ BETWEEN
 $T_1 = 10^\circ \text{C}$ AND $T_2 = 70^\circ \text{C}$.

SOLUTION:

WATER: TABLE A.5

$$\rho_1 = 1000 \text{ kg/m}^3, \quad \rho_2 = 978 \text{ kg/m}^3$$

$$\mu_1 = 1.31 \times 10^{-3} \frac{\text{N}\cdot\text{s}}{\text{m}^2}, \quad \mu_2 = 4.04 \times 10^{-4} \frac{\text{N}\cdot\text{s}}{\text{m}^2}$$

AIR: TABLE A.3

$$\rho_1 = 1.25 \text{ kg/m}^3, \quad \rho_2 = 1.03 \text{ kg/m}^3$$

$$\mu_1 = 1.76 \times 10^{-5} \frac{\text{N}\cdot\text{s}}{\text{m}^2}, \quad \mu_2 = 2.04 \times 10^{-5} \frac{\text{N}\cdot\text{s}}{\text{m}^2}$$

2.33 GIVEN: GLYCERIN AT 20°C IS

FLOWING IN A CHANNEL.

CHANNEL WIDTH : $B = 5.0 \text{ cm}$

PRESSURE GRADIENT : $\frac{dp}{dx} = -1.6 \frac{\text{kN}}{\text{m}^3}$

$$u = \frac{-1}{2\mu} \frac{dp}{dx} (By - y^2)$$

FIND: VELOCITY AND SHEAR STRESS AT
THE WALL AND 12 mm FROM THE WALL.
PLOT THE VELOCITY PROFILE.

SOLUTION: AT THE WALL ($y=0$) THE
VELOCITY IS ZERO $(u=0)$

LOOK UP VISCOSITY OF GLYCERIN
IN TABLE A.4

$$\mu = 1.41 \frac{\text{N}\cdot\text{s}}{\text{m}^2}$$

AT $y = 0.012 \text{ m}$

$$u = \frac{-1}{2(1.41)} (-1600) \left[(0.05)(0.012) - (0.012)^2 \right]$$

$$u = 0.26 \frac{\text{m}}{\text{s}}$$

SHEAR STRESS $\tau = \mu \frac{du}{dy}$

$$\frac{du}{dy} = -\frac{1}{2\mu} \frac{dp}{dx} (B - 2y)$$

$$\tau = -\frac{1}{2} \frac{dp}{dx} (B - 2y)$$

$$\text{AT } y=0 \quad \tau = -\frac{1}{2} \frac{dp}{dx} B = -\frac{1}{2} (-1600) (0.05)$$

$$\tau = 40 \frac{N}{m^2}$$

$$\text{AT } y = 0.012 \quad \tau = -\frac{1}{2} \frac{dp}{dx} (B - 2y)$$

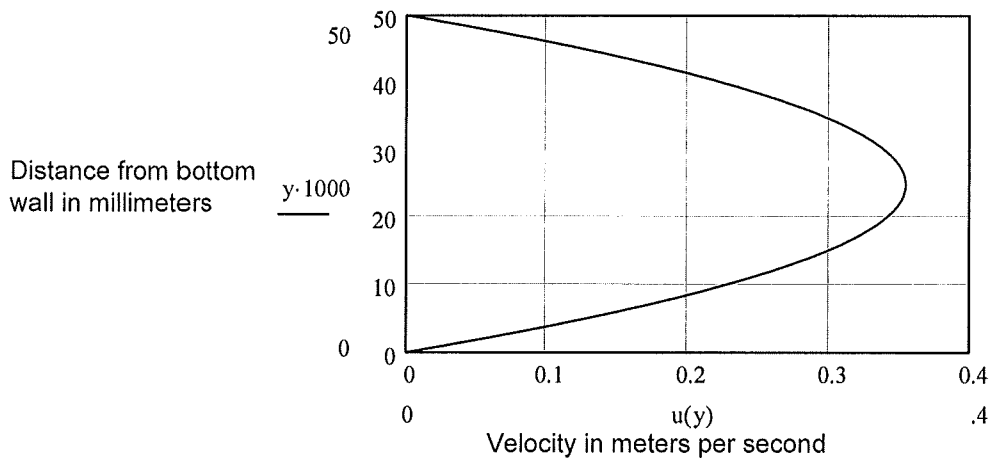
$$\tau = -\frac{1}{2} (-1600) (0.05 - 2 \cdot 0.012)$$

$$\tau = 20.8 \frac{N}{m^2}$$

Graph of Velocity Profile for Problem 2.33 (using Mathcad 2000)

- B := 0.05 channel width in meters
- $\mu := 1.41$ absolute viscosity of glycerin in Newton-seconds per meter squared
- dpdx := -1600 pressure gradient in Newtons per meter cubed
- y := 0, .0005.. .05 distance from bottom of channel in meters

$$u(y) := -\frac{1}{2 \cdot \mu} \cdot dpdx \cdot (B \cdot y - y^2)$$



2.45

GIVEN: WATER AT STANDARD CONDITIONS
FILLS A 1000 cm^3 CONTAINER.
A PRESSURE OF $2 \times 10^6 \text{ N/m}^2$ IS
APPLIED.

FIND: "ESTIMATE OF WATER
VOLUME AFTER PRESSURE HAS
BEEN APPLIED.

SOLUTION:

DEFINITION OF BULK MODULUS.

$$E_v = - \frac{dp}{dV/V}$$

$$E_v = 2.2 \text{ GN/m}^2 \text{ FOR WATER (PAGE 21, TEXT)}$$

$$dV = - \frac{dp}{E_v} V = - \frac{2 \times 10^6 \frac{\text{N}}{\text{m}^2}}{2.2 \times 10^9 \frac{\text{N}}{\text{m}^2}} (1000 \text{ cm}^3)$$

$$dV = -0.909 \text{ cm}^3$$

$$V_f = V_i + dV = 1000 \text{ cm}^3 - 0.909 \text{ cm}^3$$

$$V_f = 999.1 \text{ cm}^3$$