

11.36

GIVEN: HIGH SPEED TRAIN OF PROBLEM 9.69.  $C_{D, \text{FORM}} = 0.80$  AND TOTAL FORCE TO OVERCOME BEARING RESISTANCE IS 3000 N.

$$A_p = 9 \text{ m}^2, \quad V_{01} = 100 \text{ km/HR AND } V_{02} = 200 \text{ km/HR}$$

FIND: TOTAL RESISTANCE OF TRAIN.

% DUE TO BEARINGS, FORM DRAG, AND SKIN FRICTION DRAG.

SOLUTION: SKIN FRICTION DRAG WAS CALCULATED IN PROBLEM 9.72

$$(a) \quad F_{S1} = 1353 \text{ N}$$

$$(b) \quad F_{S2} = 5006 \text{ N}$$

$$\text{FORM DRAG} \quad F_{D, \text{FORM}} = C_{D, \text{FORM}} \left( \frac{1}{2} \rho V_0^2 \right) A_p$$

$$T = 10^\circ \text{C}, \quad \rho = 1.25 \frac{\text{kg}}{\text{m}^3}, \quad \text{AND} \quad A_p = 9 \text{ m}^2$$

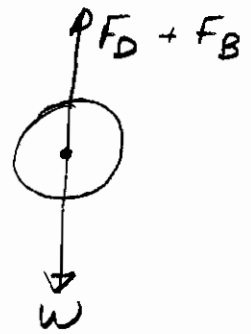
$$(a) \quad F_{DF1} = 3472 \text{ N}$$

$$(b) \quad F_{DF2} = 13889 \text{ N}$$

	$V_0$	$F_{\text{TOT}}$	% BEARINGS	% FORM	% S.F.
(a)	100 km/HR	7,825 N	38%	45%	17%
(b)	200 km/HR	21,895 N	14%	63%	23%

11.45 (1)

GIVEN: 0.5 CM HALLSTONE FALLS  
IN AIR AT 96 kPa ABSOLUTE  
AT 0°C,  $\gamma = 6 \text{ kN/m}^3$



FIND: TERMINAL VELOCITY

SOLUTION:  $\sum F_z = 0$        ~~$F_D + F_B$~~  -  ~~$W$~~  = 0       $\rightarrow$  NEGLECT

$$F_D = W \quad \frac{1}{2} \rho_{\text{AIR}} V_0^2 C_D A_p = \gamma V$$

$$V_0 = \sqrt{\frac{2 \gamma V}{\rho_{\text{AIR}} C_D A_p}}$$

$$\rho_{\text{AIR}} = \frac{96,000}{(287)(273)}$$

$$\rho_{\text{AIR}} = 1.225 \frac{\text{kg}}{\text{m}^3}$$

$$V_0 = \sqrt{\frac{2 \gamma \frac{4}{3} \pi r^3}{\rho_{\text{AIR}} C_D \pi r^2}}$$

$$V_0 = \sqrt{\frac{8 \gamma r}{3 \rho_{\text{AIR}} C_D}}$$

GUESS  $C_D = 1$ ,  $V_0 = \sqrt{\frac{8 (6000)(0.0025)}{3 (1.225)}}$

$$V_0 = 5.7 \text{ m/s}, \quad Re = \frac{(0.005)(5.7)}{1.33 \times 10^{-5}} = 2148$$

ENTER FIGURE 11.11 WITH  $Re = 2148$

FIND  $C_D \approx 0.4$

11.45 (2)

FIND  $V_0$  WITH  $C_D = 0.4$

$V_0 = 9.0 \text{ m/s} \approx 20 \text{ MPH}$

PIPER (1)

PIPER J-3 "CUB"

FIRST PROTOTYPE  
COMPLETED IN 1938

COST  $\approx$  \$1000

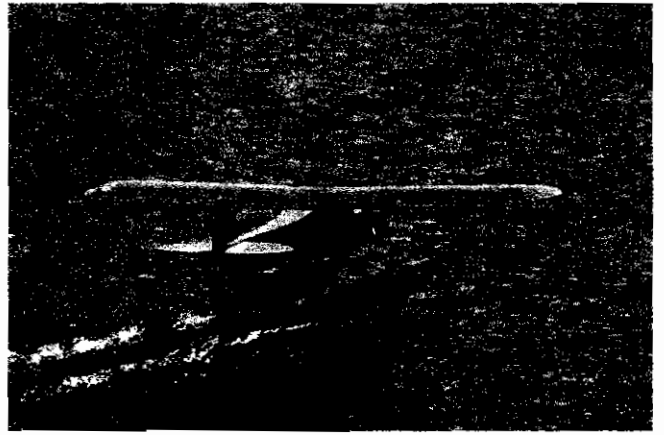
WINGSPAN  $\approx$  35' 3"

WING AREA  $\approx$  178.5 FT<sup>2</sup>

MAX TAKEOFF WEIGHT  $\approx$  1220 LBF

POWERPLANT  $\approx$  CONTINENTAL FLAT FOUR  $\approx$  65 HP

MAX SPEED  $\approx$  75 MPH



GIVEN: R.C. MODEL OF PIPER J-3

$L = 61''$  AND  $C = 9''$

FIND: (a) SCALE OF MODEL

(b) MAX LIFT FORCE OF  
MODEL AT 50 MPH

(c) DRAG FORCE AND POWER  
REQUIRED AT MAX LIFT  
AT 50 MPH

PIPER (2)

$$(a) \quad \frac{L_m}{L_p} = \frac{61''}{423''} = .144 \approx \frac{1}{7} \text{ SCALE}$$

CHECK WING AREA SCALE

$$A_m = \frac{61.9}{144} = 3.81 \text{ FT}^2$$

$$\frac{A_m}{A_p} = \frac{3.81}{178.5} = .0214$$

$$\left(\frac{L_m}{L_p}\right)^2 = .144^2 = .0207$$

VERY CLOSE

$$(b) \quad F_L = \frac{1}{2} \rho V_0^2 C_L S$$

USE FIGURE 11.23 TO OBTAIN  $C_L$

$$\text{ASPECT RATIO: } \Lambda = \frac{b}{c} = \frac{L}{c}$$

$$\Lambda = \frac{61}{9} = 6.8 \Rightarrow \text{USE } \Lambda = 7 \text{ CURVE}$$

ON FIGURE 11.23. MAXIMUM  $C_L$  IS

APPROXIMATELY 1.15.

$$\rho = .00237 \frac{\text{SLUGS}}{\text{FT}^3} \quad @ \quad 60^\circ\text{F} \ \& \ \text{SEA LEVEL}$$

$$F_L = \frac{1}{2} (.00237) (50)^2 \left(\frac{5280}{3600}\right)^2 (1.15) \left(\frac{9}{12}\right) \left(\frac{61}{12}\right)$$

$$F_L = 27.9 \text{ LB}_f$$

PIPER (3)

NOTE THAT  $F_L$  SHOULD SCALE  
BY WING AREA RATIO

$\frac{27.9}{.0214} = 1306 \text{ Lbf}$  WHICH IS  
CLOSE TO MAX TAKEOFF WEIGHT  
SPECIFICATION OF 1220 Lbf.

$$(c) F_D = \frac{1}{2} \rho V_0^2 C_D S$$

FIGURE 11.23,  $\Lambda = 7$  CURVE

$$\Rightarrow C_D \approx 0.11$$

$$F_D = 2.67 \text{ Lbf}$$

$$P = F_D V_0 = 2.67 (50) \left( \frac{5280}{3600} \right)$$

$$P = 196 \frac{\text{FT-Lbf}}{\text{S}} = 0.36 \text{ hp}$$

HOW WILL POWER SCALE?