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| Log Volumes: Geometric Solids |  |  |
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| $\text { TOP } \begin{aligned} & \text { PARABOLOID } \\ & \text { ORCONE } \end{aligned}$ |  |  |
|  |  | Logs are not perfect cylinders! |
| UPPERLOGS | FRUSTUM OF PARABOLOID | Logs taper from one end to another |
|  |  | Truncated sections of a tree can be approximated as geometric shapes: |
| ${ }_{\text {butr }}$ | ( ${ }_{\text {FRUSTUM OF }}^{\text {NELLID }}$ | - Cone |
| Stump + .-...-- |  | - Neiloid |
| where $B_{1 / 2}=$ cross-sectional area at $\log$ midpoint <br> $B=$ cross-sectional area at large end of $\log$ <br> $b=$ cross-sectional area at small end of $\log$ <br> $L=$ log length |  |  |
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$B=$ cross-sectional area at large end of log
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$L=\log$ length
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| Log Volumes: Geometric Solids |  |  |
| :---: | :---: | :---: |
| Geometric Solid | Equation for Volume $V$ (cubic units) ${ }^{a}$ | Equation Number |
| Cylinder | $V=A_{b} h$ | (6-1) |
| Paraboloid | $V=\frac{1}{2}\left(A_{b} h\right)$ | (6-2) |
| Cone | $V=\frac{1}{3}\left(A_{b} h\right)$ | (6-3) |
| Neiloid | $V=\frac{1}{4}\left(A_{b} h\right)$ | (6-4) |
| Paraboloid frustum | $\begin{aligned} & V=\frac{h}{2}\left(A_{b}+A_{u}\right) \quad \text { (Smalian's formula) } \\ & V=A_{m} h \quad \text { (Huber's formula) } \end{aligned}$ | $\begin{aligned} & (6-5) \\ & (6-6) \end{aligned}$ |
| Cone frustum | $V=\frac{h}{3}\left(A_{b}+\sqrt{A_{b} A_{u}}+A_{u}\right)$ | (6-7) |
| Neiloid frustum | $V=\frac{h}{4}\left(A_{b}+\sqrt[3]{A_{b}^{2} A_{u}}+\sqrt[3]{A_{b} A_{u}^{2}}+A_{u}\right)$ | (6-8) |
| Neiloid, cone, or paraboloid frustum | $V=\frac{h}{6}\left(A_{b}+4 A_{m}+A_{u}\right) \quad$ (Newton's formula) | (6-9) |
| ${ }^{a} A_{b}$, cross-sectional area at base; $A_{m}$, cross-sectional area at middle; $A_{u}$, cross-sectional area at upper end; $h$, height or length. |  |  |


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