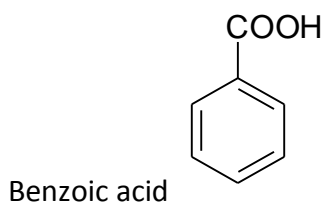


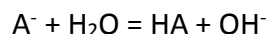
## 2 – Equilibria Problem Set

### The Basics

- 1] Calculate the solubility of  $\text{PbCl}_2$  ( $K_{\text{sp}} = 1.7 \times 10^{-5}$ ) in the presence of 0.122 M NaCl. <sup>1</sup>
- 2] Calculate the  $K_{\text{sp}}$  of barium sulfate (MW 233) if its solubility is measured as 0.0023 mg/mL. <sup>2</sup>
- 3] What is the molar solubility of  $\text{PbCl}_2$ ,  $K_{\text{sp}} = 1.7 \times 10^{-5}$ ? <sup>3</sup>
- 4] What is the solubility of barium carbonate? <sup>4</sup>  $\text{BaCO}_3$   $K_{\text{sp}} = 5.0 \times 10^{-9}$
- 5] What is the solubility of copper (I) sulfide in 0.1 M  $\text{Na}_2\text{S}$ ? <sup>5</sup>  $\text{Cu}_2\text{S}$   $K_{\text{sp}} = 3 \times 10^{-49}$
- 6] What is the solubility of  $\text{PbCl}_2$  in 0.10 M NaCl? <sup>6</sup>
- 7] Calculate the pH of a solution of 0.025 M acetic acid and 0.025 M sodium acetate. <sup>7</sup>
- 8] What the pH of  $[\text{H}^+] = 3.35 \times 10^{-6}$ ? <sup>8</sup>
- 9] Calculate the pH of a solution of 0.025 M acetic acid,  $K_{\text{a}} = 1.8 \times 10^{-5}$  <sup>9</sup>
- 10] What is the pH of a solution of 0.100 M HCl? <sup>10</sup>
- 11] What is the pH of 0.10 M benzoic acid? <sup>11</sup>  $K_{\text{a}} = 6.28 \times 10^{-5}$



- 12] The concentration of  $\text{H}^+$  in a pH 6.772 solution is \_\_\_\_\_ <sup>12</sup>
  - 13] The pH of a solution of a 0.100 M weak acid (HA)  $K_{\text{a}} = 2.7 \times 10^{-6}$  is \_\_\_\_\_ <sup>13</sup>
  - 14] What is  $[\text{H}^+]$  when a solution is pH = 4.653? <sup>14</sup>
  - 15] The solubility of the salt  $\text{MA}_2$  ( $K_{\text{sp}} = 8.9 \times 10^{-17}$ ) is \_\_\_\_\_ <sup>15</sup>
- $$\text{MA(s)} = \text{M}^{2+}(\text{aq}) + 2\text{A}^{-}(\text{aq})$$
- 16] What is the solubility of a salt, AB ( $K_{\text{sp}} = 7.2 \times 10^{-12}$ ) in the presence of 0.10 M  $\text{B}^{-}$ ? <sup>16</sup>
  - 17] The  $K_{\text{a}}$  of a weak acid (HA) is  $7.2 \times 10^{-6}$ . What is  $K_{\text{b}}$  for the following reaction? <sup>17</sup>

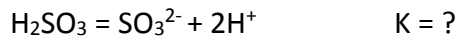


18] The concentration of  $H^+$  in a pH 8.55 solution is <sup>18</sup>

19] What is the pH of a 2.11 M solution of  $HNO_3$ ? <sup>19</sup>

20] What is the  $H^+$  concentration of a solution that has a pH of 5.32? <sup>20</sup>

21] What is K for this reaction? <sup>21</sup>



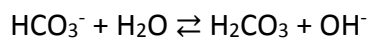
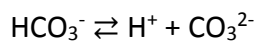
### Charge Balance and Mass Balance

22] Write down a valid mass balance for a solution for 0.10 M  $NaHCO_3$ . <sup>22</sup>

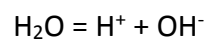
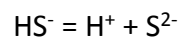
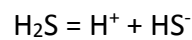
23] What is the charge balance for a solution of 0.1 M  $MgCl_2$ ? <sup>23</sup>

24] What is the charge balance for a solution of 0.10 M  $NaHCO_3$ ? <sup>24</sup>

$$K_{a1} = 6.352 \quad K_{a2} = 10.329$$

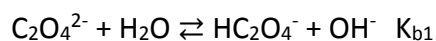
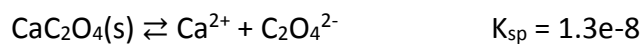


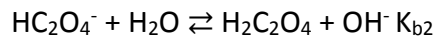
25] What is the CBE for the follow reaction sequence? <sup>25</sup>



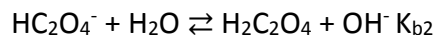
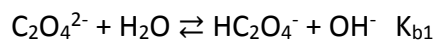
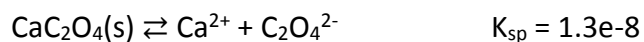
26] Write a charge balance equation for a solution containing  $NaNO_3$ ,  $KCl$ , and  $Na_2SO_4$ . <sup>26</sup>

27] What is the mass balance equation for the following sequence of reactions? <sup>27</sup>

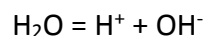
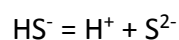
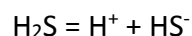




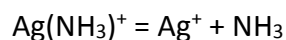
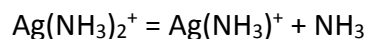
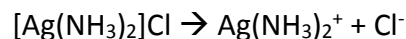
28] What is the charge balance equation for the reaction sequence: <sup>28</sup>



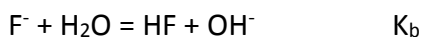
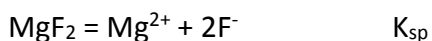
29] What is the CBE for the follow reaction sequence? <sup>29</sup>



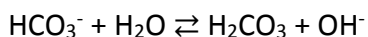
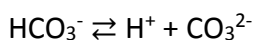
30] What is the MBE for 1.00e-3 M  $[\text{Ag}(\text{NH}_3)_2]\text{Cl}$  for the following reaction sequence: <sup>30</sup>



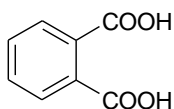
31] What is the MBE for the following sequence of reactions? <sup>31</sup>



32] What is the charge balance for a solution of 0.10 M  $\text{NaHCO}_3$ ? <sup>32</sup>



33] Write a charge balance equation of for a solution of 0.10 M phthalic acid. <sup>33</sup>



$$K_{a1} = 1.12 \times 10^{-3} \quad K_{a2} = 3.90 \times 10^{-6}$$

34] What is the charge balance equation for a solution that is saturated with  $\text{SrF}_2$ ? <sup>34</sup>

$$K_{sp}(\text{SrF}_2) = 2.9 \times 10^{-9} \quad K_a(\text{HF}) = 6.8 \times 10^{-4}$$

35] What is the mass balance equation for a solution that is initially 0.1 M NaF?  $K_a(\text{HF}) = 6.8 \times 10^{-4}$  <sup>35</sup>

### Solubility

36] What is the solubility of  $\text{SrF}_2$  ( $K_{sp} = 2.8 \times 10^{-9}$ ) at pH 4.00?  $\text{HF } K_a = 6.76 \times 10^{-4}$ . <sup>36</sup>

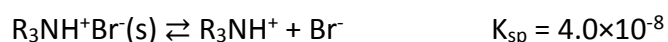
37] What best explains the solubility of  $\text{Ag}_2\text{SO}_4$ ? <sup>37</sup>

38] What is the molar solubility of  $\text{BaF}_2$  ( $K_{sp} = 1.7 \times 10^{-6}$ ) at pH 7.20?  $K_a(\text{HF}) = 6.8 \times 10^{-4}$  <sup>38</sup>

39] What is the solubility of  $\text{Hg}_2\text{Cl}_2$  ( $K_{sp} = 1.2 \times 10^{-18}$ ) in 0.20 M NaCl? <sup>39</sup>

40] The  $K_{sp}$  of  $\text{PbI}_2$  is  $7.9 \times 10^{-9}$ . What is the concentration of  $\text{I}^-$  required to precipitate 99.99% of  $1.6 \times 10^{-4}$  M  $\text{Pb}^{2+}(\text{aq})$ ? <sup>40</sup>

41] Consider a saturated solution of  $\text{R}_3\text{NH}^+\text{Br}^-$ , where R is an organic group. Find the solubility of  $\text{R}_3\text{NH}^+\text{Br}^-$  in a solution maintained at pH 9.50. <sup>41</sup>



42] What is the aqueous solubility of AgCl at pH 4.00 ( $K_{sp} = 1.8 \times 10^{-11}$ )? <sup>42</sup>

43] A mixture of AgCl (MW 143.35,  $K_{sp} = 1.8 \times 10^{-10}$ ) and AgBr (MW 187.9,  $K_{sp} = 5.0 \times 10^{-13}$ ) weighs 2.000 g. This mixture is reduced to silver metal (AW 107.9), which weighs 1.300 g. Calculate the mass of AgCl in the original sample. <sup>43</sup>

44] A 0.2795 g sample of the insecticide containing lindane ( $\text{C}_6\text{H}_6\text{Cl}_6$ , MW 290.8) and DDT ( $\text{C}_{14}\text{H}_9\text{Cl}_5$ , MW 354.5) was burned in purified air. The products of this reaction,  $\text{CO}_2$ ,  $\text{H}_2\text{O}$ , and HCl were passed through a solution of  $\text{NaHCO}_3$  that captured HCl. Chloride was precipitated as AgCl with a solution of excess  $\text{AgNO}_3(\text{aq})$ . The AgCl was dried and weighed, 0.7161 g. Calculate the percent lindane and DDT in the sample. <sup>44</sup>

45] Calculate the concentration of  $\text{Ba}^{2+}$  in solution when 15.00-mL of 0.200 M  $\text{K}_2\text{CrO}_4(\text{aq})$  is added to 25.00-mL of 0.100 M  $\text{BaCl}_2(\text{aq})$ .<sup>45</sup>

46] What is the solubility of  $\text{CaF}_2$  in 0.100 M HCl. What are the equilibrium concentrations HF and  $\text{F}^-$  under these conditions?<sup>46</sup>

47] What is the solubility of  $\text{MgCO}_3$  at pH 5.00?<sup>47</sup>

48] The  $K_{\text{sp}}$  of  $\text{AgCl}$  is  $1.8 \times 10^{-10}$ . What is the concentration of  $\text{Cl}^-$  required to remove 99.99% of  $1.0 \times 10^{-3}$  M  $\text{Ag}^+$ ?<sup>48</sup>

49] The  $K_{\text{sp}}$  of  $\text{AgCN}(\text{s})$  is  $2.2 \times 10^{-16}$ . The  $K_{\text{a}}$  of HCN is  $6.2 \times 10^{-10}$ . What would you expect with  $\text{AgCN}$  molar solubility and pH?<sup>49</sup>

## Answers

<sup>1</sup>  $x(0.122+2x)^2=1.7 \times 10^{-5}$ ;  $x=1.7 \times 10^{-5}/(0.122+2x)^2$ ; let  $2x=0$ ;  $x_1=1.14 \times 10^{-3}$  then  $x_2=1.10 \times 10^{-3}$  and  $x_3=1.10 \times 10^{-3}$

<sup>2</sup>  $9.7 \times 10^{-11}$

<sup>3</sup>  $K_{\text{sp}} = [\text{Pb}^{2+}][\text{Cl}^-]^2 \quad (2x)^2x = 1.7 \times 10^{-5} \quad x = 1.6 \times 10^{-2} \text{ M}$

4	$\text{BaCO}_3$	=	$\text{Ba}^{2+}$	+	$\text{CO}_3^{2-}$
	--		0		0
	--		+x		+x
	--		x		x

$x^2 = 5.0 \times 10^{-9}$

$x = 7.1 \times 10^{-5} \text{ M}$

5	$\text{Cu}_2\text{S}$	=	$2\text{Cu}^+$	+	$\text{S}^{2-}$
	--		0		0.1 M
	--		+2x		+x
	--		2x		0.1 + x

$(2x)^2(0.1+x) \cong 4x^2(0.1) = 3 \times 10^{-49}$

$x = 9 \times 10^{-25}$

<sup>6</sup>  $(0.10 + 2x)^2 x = 1.7 \times 10^{-5}$ ;  $(0.10)^2 x \approx 1.7 \times 10^{-5}$ ;  $x = 1.7 \times 10^{-3} \text{ M}$

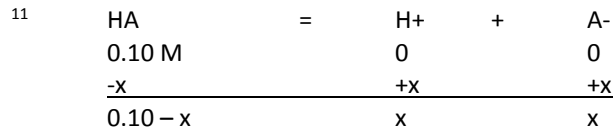
<sup>7</sup> 4.74

<sup>8</sup>  $\text{pH} = -\log(3.35 \times 10^{-6}) = 5.475$

<sup>9</sup> 3.17

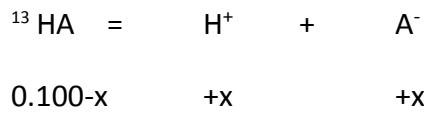
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<sup>10</sup> 1.000      be careful of s.f.



$$x^2/(0.10 - x) \cong x^2/0.10 = 6.28e-5 \quad x = [H^+] = 2.5e-3 \quad \text{pH} = 2.60$$

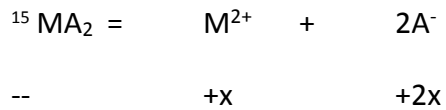
<sup>12</sup>  $1.69 \times 10^{-7}$  M



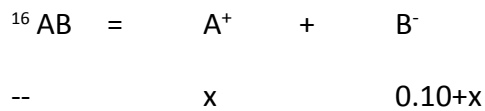
$$x^2/0.100-x = 2.7e-6 \quad x = 5.2e-4 \text{ M}$$

pH = 3.28

<sup>14</sup> pH = 4.653       $[H^+] = 10^{-4.653} = 2.22e-5 \text{ M}$



$$(2x)^2x = 8.9e-17 \quad x = 2.8e-6 \text{ M}$$



$$x(0.10+x) \approx 0.10x = 7.2e-12$$

$$x = 7.2e-11 \text{ M}$$

<sup>17</sup>  $K_a K_b = K_w$        $K_b = 1.00e-14/7.2e-6 = 1.4e-9$

<sup>18</sup>  $2.8e-9$  M watch S.F.

<sup>19</sup> -0.324 watch S.F.

<sup>20</sup>  $4.8 \times 10^6$  M watch S.F.

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<sup>21</sup>  $8.1e-10$

<sup>22</sup>  $0.10 \text{ M} = [\text{H}_2\text{CO}_3] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}]$

<sup>23</sup>  $2[\text{Mg}^{2+}] = [\text{Cl}^-]$

<sup>24</sup>  $[\text{Na}^+] + [\text{H}^+] = [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}] + [\text{OH}^-]$

<sup>25</sup>  $[\text{H}^+] = [\text{OH}^-] + [\text{HS}^-] + 2[\text{S}^{2-}]$

<sup>26</sup>  $[\text{Na}^+] + [\text{K}^+] = [\text{NO}_3^-] + [\text{Cl}^-] + 2[\text{SO}_4^{2-}]$

<sup>27</sup>  $[\text{Ca}^{2+}] = [\text{C}_2\text{O}_4^{2-}] + [\text{HC}_2\text{O}_4^-] + [\text{H}_2\text{C}_2\text{O}_4]$

<sup>28</sup>  $2[\text{Ca}^{2+}] = 2[\text{C}_2\text{O}_4^{2-}] + [\text{HC}_2\text{O}_4^-] + [\text{OH}^-]$

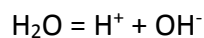
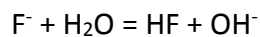
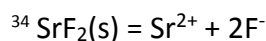
<sup>29</sup>  $[\text{H}^+] = [\text{OH}^-] + [\text{HS}^-] + 2[\text{S}^{2-}]$

<sup>30</sup>  $1.00e-3 \text{ M} = [\text{Ag}(\text{NH}_3)_2^+] + [\text{Ag}(\text{NH}_3)^+] + [\text{Ag}^+]$

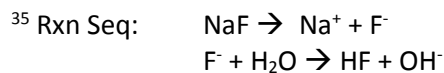
<sup>31</sup>  $2[\text{Mg}^{2+}] + 2[\text{Mg}(\text{OH})^+] = [\text{F}^-] + [\text{HF}]$

<sup>32</sup>  $[\text{Na}^+] + [\text{H}^+] = [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}] + [\text{OH}^-]$

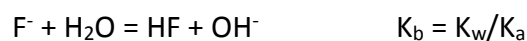
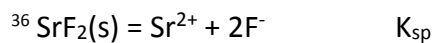
<sup>33</sup>  $[\text{H}^+] = 2[\text{A}^{2-}] + [\text{HA}^-]$



CBE:  $2[\text{Sr}^{2+}] + [\text{H}^+] = [\text{F}^-] + [\text{OH}^-]$



**MBE:  $0.1 \text{ M} = [\text{Na}^+] = [\text{F}^-] + [\text{HF}]$**



MBE:  $2[\text{Sr}^{2+}] = [\text{F}^-] + [\text{HF}]$

$\text{pH} = 4.00 \rightarrow [\text{OH}^-] = 1.0e-10 \text{ M}$

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$$K_b = \frac{[\text{HF}][\text{OH}^-]}{[\text{F}^-]} \rightarrow [\text{HF}] = 0.1479 [\text{F}^-]$$

$$2[\text{Sr}^{2+}] = [\text{F}^-] + [\text{HF}] = 1.1479 [\text{F}^-] \quad \#1$$

$$K_{sp} = [\text{Sr}^{2+}][\text{F}^-]^2 \rightarrow [\text{F}^-] = (K_{sp}/[\text{Sr}^{2+}])^{1/2} \quad \#2$$

Sub 2 into 1

$$2[\text{Sr}^{2+}] = 1.1479(K_{sp}/[\text{Sr}^{2+}])^{1/2} \quad [\text{Sr}^{2+}]^3 = 9.52\text{e-}10 \quad [\text{Sr}^{2+}] = s = 9.8\text{e-}4 \text{ M}$$

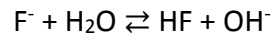
$$^{37} [\text{Ag}^+]/2 \quad \text{or} \quad [\text{SO}_4^{2-}]$$

$$^{38} \text{MBE: } 2[\text{Ba}^{2+}] = [\text{F}^-] + [\text{HF}] \quad \& \quad [\text{H}^+] = 6.31\text{e-}8 \text{ M}; [\text{OH}^-] = 1.58\text{e-}7$$

$$K_{sp} = [\text{Ba}^{2+}][\text{F}^-]^2 = 1.7\text{e-}6$$

$$K_a(\text{HF}) = \frac{[\text{H}^+][\text{F}^-]}{[\text{HF}]} = 6.8\text{e-}4$$

3 variables:  $[\text{Ba}^{2+}]$ ,  $[\text{F}^-]$ ,  $[\text{HF}]$



$$K_b = K_w/K_a = 1.00\text{e-}14/6.8\text{e-}4 = 1.47\text{e-}11$$

Using  $K_b$  solve for  $[\text{HF}]$

$$[\text{HF}] = K_b[\text{F}^-]/[\text{OH}^-] \quad \text{will sub into MBE}$$

$$2[\text{Ba}^{2+}] = [\text{F}^-] + [\text{HF}]$$

$$2[\text{Ba}^{2+}] = [\text{F}^-] + K_b[\text{F}^-]/[\text{OH}^-]$$

Sub all knowns into above

$$2[\text{Ba}^{2+}] = [\text{F}^-] + 1.47\text{e-}11 * [\text{F}^-]/1.58\text{e-}7$$

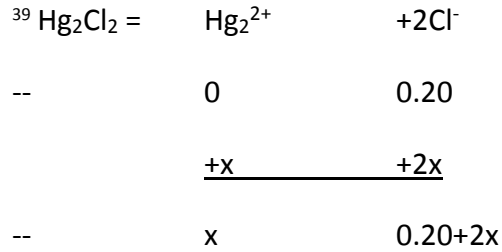
$$2[\text{Ba}^{2+}] \cong [\text{F}^-] \quad \text{sub into } K_{sp}$$



---


$$K_{sp} = [\text{Ba}^{2+}][\text{F}^-]^2 = [\text{Ba}^{2+}](2[\text{Ba}^{2+}])^2$$

$$[\text{Ba}^{2+}] = (K_{sp}/4)^{1/3} = 7.5\text{e-}3\text{M}$$



$$1.2 \times 10^{-18} = x(0.20+2x)^2$$

$$1.2 \times 10^{-18} \approx x(0.20)^2$$

$$x = 3.0\text{e-}17$$

$$^{40} 7.9\text{e-}9 = (1-0.9999)[1.6\text{e-}4][\text{I}^-]^2 \quad [\text{I}^-] = 0.70 \text{ M}$$

$$^{41} \text{MBE:} \quad [\text{Br}^-] = [\text{R}_3\text{NH}^+] + [\text{R}_3\text{N}] \quad \#1$$

$$K_a = [\text{H}^+][\text{R}_3\text{N}]/[\text{R}_3\text{NH}^+] \quad \#2$$

$$K_{sp} = [\text{R}_3\text{NH}^+][\text{Br}^-] \quad \#3$$

3 variables, 3 eqn

$$[\text{H}^+] = 10^{-9.50} = 3.2\text{e-}10$$

If solve for [Br<sup>-</sup>] we find the solubility of R<sub>3</sub>NH<sup>+</sup>Br<sup>-</sup>

Sub into MBE narrow it down to 2 variables

$$[\text{R}_3\text{N}] = [\text{R}_3\text{NH}^+]$$

$$K_a/[\text{H}^+] = 7.19 [\text{R}_3\text{NH}^+]$$

$$[\text{Br}^-] = [\text{R}_3\text{NH}^+] + [\text{R}_3\text{N}]$$

$$[\text{Br}^-] = [\text{R}_3\text{NH}^+] + 7.19 [\text{R}_3\text{NH}^+]$$

$$= 8.19 [\text{R}_3\text{NH}^+]$$

$$[\text{R}_3\text{NH}^+] = [\text{Br}^-] / 8.19$$

Sub into K<sub>sp</sub>

---

$$K_{sp} = [R_3NH^+][Br^-] = 4.0 \times 10^{-8}$$

$$= [Br^-]^2 / 8.19$$

$$[Br^-] = 5.7e-4$$



$$K_{sp} = x^2 = 1.8e-11 \quad x = 4.2e-6$$

$$^{43} x \text{ g AgCl} + y \text{ g AgBr} = 2.000 \text{ g}$$

$$x \text{ g AgCl} * (\text{mol AgCl} / 143.35 \text{ g}) * (\text{mol Ag} / \text{mol AgCl}) * (107.9 \text{ g/mol}) = 0.7527x \text{ g Ag}$$

$$y \text{ g AgBr} * (\text{mol AgBr} / 187.9 \text{ g}) * (\text{mol Ag} / \text{mol AgBr}) * (107.9 \text{ g/mol}) = 0.5742y \text{ g Ag}$$

$$0.7527x \text{ g Ag} + 0.5742y \text{ g Ag} = 1.300 \text{ g}$$

$$y = 2.000 - x \quad \text{sub into above}$$

$$0.7527x + 0.5742(2.000 - x) = 1.300 \text{ g}$$

$$\text{mass Ag} = 0.849 \text{ g}$$

<sup>44</sup> 2 equations:

$$\text{Mass lindane} + \text{Mass DDT} = 0.2795 \text{ g} \quad \#1$$

$$\text{Mass AgCl from lindane} + \text{Mass AgCl from DDT} = 0.7161 \text{ g} \quad \#2$$

Let  $x = \text{mass lindane}$  and  $y = \text{mass DDT}$

$$x + y = 0.2795 \quad \#3$$

$$\text{mass AgCl from lindane} = x \times \frac{\text{mol lindane}}{290.8 \text{ g}} \times \frac{6 \text{ mol AgCl}}{\text{mol lindane}} \times \frac{143.35 \text{ g}}{\text{mol AgCl}} = 2.958x$$

$$\text{mass AgCl from DDT} = y \times \frac{\text{mol DDT}}{354.5 \text{ g}} \times \frac{5 \text{ mol AgCl}}{\text{mol DDT}} \times \frac{143.35 \text{ g}}{\text{mol AgCl}} = 2.022y$$

$$\text{Sub into \#3 we have} \quad 2.958x + 2.022y = 0.7161 \quad \#4$$

$$\text{Solve for } x \text{ in \#3} \quad x = 0.2795 - y \text{ and sub into \#4}$$

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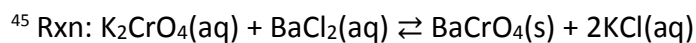
$$2.958(0.2795 - y) + 2.022y = 0.7161$$

$$y = 0.1183 \text{ g DDT}$$

$$x = 0.1612 \text{ g lindane}$$

$$\% \text{ lindane} = 0.1612/0.2795 * 100 = 57.68\%$$

$$\% \text{ DDT} = 100 - 57.68 = 42.31 \%$$



Must find limiting reagent.

$$25.00\text{-mL} * 0.100 \text{ M BaCl}_2 = 2.50 \text{ mmol Ba}^{2+}$$

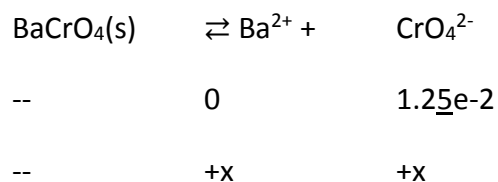
$$15.00\text{-mL of } 0.200 \text{ M K}_2\text{CrO}_4 = 3.00 \text{ mmol CrO}_4^{2-}$$

2.00 mmol  $\text{Ba}^{2+}$  must limiting reagent. Left over  $\text{CrO}_4^{2-}$ :

$$3.00 - 2.50 \text{ mmol} = 0.50 \text{ mmol CrO}_4^{2-}$$

$$[\text{CrO}_4^{2-}] = 0.50 \text{ mmol}/40.0\text{-mL} = 1.25 \times 10^{-2} \text{ M}$$

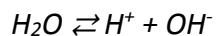
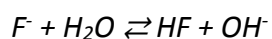
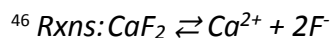
Solubility Reaction:



$$K_{\text{sp}} = 2.1 \times 10^{-10}$$

$$2.1 \times 10^{-10} = x(1.25 \times 10^{-2} - x) \cong x(1.25 \times 10^{-2})$$

$$x = 1.7 \times 10^{-8} \text{ M}$$



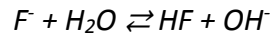
$$\text{MBE: } 2[\text{Ca}^{2+}] = [\text{F}^-] + [\text{HF}] \quad \&$$

---

$$[H^+] = 0.100 \text{ M}; [OH^-] = 1.00e-13$$

$$K_{sp} = [Ca^{2+}][F^-]^2 = 3.9e-11 \quad K_a$$

$$[HF] = [H^+][F^-]/[HF] = 6.8e-4$$



$$K_b = K_w/K_a$$

$$= 1.00e-14/6.8e-4 = 1.47e-11$$

Using  $K_b$  solve for  $[HF]$

$$[HF] = K_b[F^-]/[OH^-] \quad \text{will sub into MBE}$$

$$2[Ca^{2+}] = [F^-] + [HF]$$

$$2[Ca^{2+}] = [F^-] + K_b[F^-]/[OH^-]$$

Sub all knowns into above

$$2 [Ca^{2+}] = [F^-] + 1.47e-11 * [F^-]/1.00e-13$$

$$2 [Ca^{2+}] = [F^-] + 147[F^-] = 148 [F^-]$$

$$[Ca^{2+}][F^-]^2 = 3.9e-11$$

$$74 [F^-]^3 = 3.9e-11$$

$$[F^-] = 8.08 e-5$$

From  $K_a$

$$[HF] = [H^+][F^-]/6.8e-4$$

$$= 1.00e-1 * 8.08e-5 / 6.8e-4$$

$$[HF] = 1.2e-2$$

$$\text{From MBE} \quad [Ca^{2+}] = \frac{1}{2} [F^-] + \frac{1}{2} [HF]$$

$$= \frac{1}{2} * 8.1e-5 + \frac{1}{2} * 1.2e-2 = 6.0e-3$$

From  $K_{sp}$

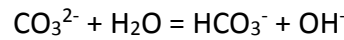
$$[Ca^{2+}] = 3.9e-11/[F^-]^2 = 3.9e-11/8.08e-5^2 = 6.0e-3$$

---

<sup>47</sup> MBE:  $[\text{Mg}^{2+}] = [\text{CO}_3^{2-}] + [\text{HCO}_3^-] + [\text{H}_2\text{CO}_3]$

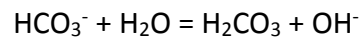
$$[\text{OH}^-] = 1.00\text{e-}9$$

$$K_{\text{sp}} = [\text{Mg}^{2+}][\text{CO}_3^{2-}] = 3.5\text{e-}8$$



$$K_{\text{b1}} = K_{\text{w}}/K_{\text{a2}} = 1.00\text{e-}14/4.69\text{e-}11 =$$

$$2.13\text{e-}4 = [\text{HCO}_3^-][\text{OH}^-]/[\text{CO}_3^{2-}]$$



$$K_{\text{b2}} = K_{\text{w}}/K_{\text{a1}} = 1.00\text{e-}14/4.45\text{e-}7 =$$

$$2.25\text{e-}8 = [\text{H}_2\text{CO}_3][\text{OH}^-]/[\text{HCO}_3^-]$$

Using  $K_{\text{b1}}$  solve for  $[\text{HCO}_3^-]$

$$[\text{HCO}_3^-] = K_{\text{b1}}[\text{CO}_3^{2-}]/[\text{OH}^-]$$

will sub into MBE

Using  $K_{\text{b2}}$  solve for  $[\text{H}_2\text{CO}_3]$

$$[\text{H}_2\text{CO}_3] = K_{\text{b2}} [\text{HCO}_3^-]/[\text{OH}^-]$$

$$= K_{\text{b1}}K_{\text{b2}}[\text{CO}_3^{2-}]/[\text{OH}^-]^2$$

Sub both of above into MBE

$$[\text{Mg}^{2+}] = [\text{CO}_3^{2-}] + [\text{HCO}_3^-] + [\text{H}_2\text{CO}_3]$$

$$[\text{Mg}^{2+}] = [\text{CO}_3^{2-}] + K_{\text{b1}}[\text{CO}_3^{2-}]/[\text{OH}^-] + K_{\text{b1}}K_{\text{b2}}[\text{CO}_3^{2-}]/[\text{OH}^-]^2$$

Sub all knowns into above

$$[\text{Mg}^{2+}] = [\text{CO}_3^{2-}] + 2.13\text{e-}4[\text{CO}_3^{2-}]/1.00\text{e-}9 + 2.13\text{e-}4*2.25\text{e-}8[\text{CO}_3^{2-}]/(1.00\text{e-}9)^2$$

$$[\text{Mg}^{2+}] = 2.13\text{e}5[\text{CO}_3^{2-}] + 4.79\text{e}6[\text{CO}_3^{2-}] = 5.01\text{e}6[\text{CO}_3^{2-}]$$

$$[\text{CO}_3^{2-}] = [\text{Mg}^{2+}]/5.01\text{e}6 \quad \text{sub into } K_{\text{sp}}$$

---

$$[\text{Mg}^{2+}][\text{CO}_3^{2-}] = 3.5\text{e-}8$$

$$[\text{Mg}^{2+}]^2/5.01\text{e}6 = 3.5\text{e-}8$$

$$[\text{Mg}^{2+}] = \mathbf{0.42\text{ M}}$$

$$x\text{ g AgCl} + y\text{ g AgBr} = 2.000\text{ g}$$

$$x\text{ g AgCl} * (\text{mol AgCl}/143.35\text{ g}) * (\text{mol Ag}/\text{mol AgCl}) * (107.9\text{ g}/\text{mol}) = 0.7527x\text{ g Ag}$$

$$y\text{ g AgBr} * (\text{mol AgBr}/187.9\text{ g}) * (\text{mol Ag}/\text{mol AgBr}) * (107.9\text{ g}/\text{mol}) = 0.5742y\text{ g Ag}$$

$$0.7527x\text{ g Ag} + 0.5742y\text{ g Ag} = 1.300\text{ g}$$

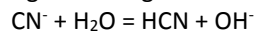
$$y = 2.000 - x \quad \text{sub into above}$$

$$0.7527x + 0.5742(2.000 - x) = 1.300\text{ g}$$

$$\text{mass Ag} = 0.849\text{ g}$$

$$^{48} K_{sp} = 1.8\text{e-}10 = [\text{Ag}^+][\text{Cl}^-] \dots 99.99\% \text{ Ag}^+ \text{ removal} \quad 1.8\text{e-}10 = (1.000 - 0.9999)(1.0\text{e-}3)[\text{Cl}^-] \quad [\text{Cl}^-] = \mathbf{1.8\text{e-}3\text{ M}}$$

<sup>49</sup> **AgCN solubility should decrease with increasing pH.**



Since OH<sup>-</sup> is a product increasing its concentration should drive the reaction to AgCN using Le Chatelier's principles