

5 – EDTA Titrations

Table 13-1 Values of $\alpha_{Y^{4-}}$ for EDTA at 20°C and $\mu = 0.10$ M

pH	$\alpha_{Y^{4-}}$
0	1.3×10^{-23}
1	1.9×10^{-18}
2	3.3×10^{-14}
3	2.6×10^{-11}
4	3.8×10^{-9}
5	3.7×10^{-7}
6	2.3×10^{-5}
7	5.0×10^{-4}
8	5.6×10^{-3}
9	5.4×10^{-2}
10	0.36
11	0.85
12	0.98
13	1.00
14	1.00

Table 13-2 Formation constants for metal-EDTA complexes

Ion	$\log K_f$	Ion	$\log K_f$	Ion	$\log K_f$
Li ⁺	2.79	Mn ³⁺	25.3 (25°C)	Ce ³⁺	15.98
Na ⁺	1.66	Fe ³⁺	25.1	Pr ³⁺	16.40
K ⁺	0.8	Co ³⁺	41.4 (25°C)	Nd ³⁺	16.61
Be ²⁺	9.2	Zr ⁴⁺	29.5	Pm ³⁺	17.0
Mg ²⁺	8.79	Hf ⁴⁺	29.5 ($\mu = 0.2$)	Sm ³⁺	17.14
Ca ²⁺	10.69	VO ²⁺	18.8	Eu ³⁺	17.35
Sr ²⁺	8.73	VO ₂ ⁺	15.55	Gd ³⁺	17.37
Ba ²⁺	7.86	Ag ⁺	7.32	Tb ³⁺	17.93
Ra ²⁺	7.1	Tl ⁺	6.54	Dy ³⁺	18.30
Sc ³⁺	23.1	Pd ²⁺	18.5 (25°C, $\mu = 0.2$)	Ho ³⁺	18.62
Y ³⁺	18.09	Zn ²⁺	16.50	Er ³⁺	18.85
La ³⁺	15.50	Cd ²⁺	16.46	Tm ³⁺	19.32
V ²⁺	12.7	Hg ²⁺	21.7	Yb ³⁺	19.51
Cr ²⁺	13.6	Sn ²⁺	18.3 ($\mu = 0$)	Lu ³⁺	19.83
Mn ²⁺	13.87	Pb ²⁺	18.04	Am ³⁺	17.8 (25°C)
Fe ²⁺	14.32	Al ³⁺	16.3	Cm ³⁺	18.1 (25°C)
Co ²⁺	16.31	Ga ³⁺	20.3	Bk ³⁺	18.5 (25°C)
Ni ²⁺	18.62	In ³⁺	25.0	Cf ³⁺	18.7 (25°C)
Cu ²⁺	18.80	Tl ³⁺	37.8 ($\mu = 1.0$)	Th ⁴⁺	23.2
Ti ³⁺	21.3 (25°C)	Bi ³⁺	27.8	U ⁴⁺	25.8
V ³⁺	26.0			Np ⁴⁺	24.6 (25°C, $\mu = 1.0$)
Cr ³⁺	23.4				

1] What is the fraction of EDTA in the Y⁴⁻ form at pH 5? ¹

2] In reference to EDTA titrations the symbol, $\alpha_{Y^{4-}}$, indicates which of the following? ²

- The fraction of metal chelated by EDTA
- The concentration of EDTA in the Y⁴⁻ form.
- The fraction of EDTA in the Y⁴⁻ form.
- The analytical concentration of metal.
- The fraction of EDTA not in the Y⁴⁻ form.

3] What is the fraction of EDTA in the Y⁴⁻ form at pH 7.00? ³

- 1.00
- 5.0e-4
- 0.36
- 0.500
- 3.3e-14

4] The conditional formation constant K_f' for CaY²⁻ is related to K_f through which of the relationships? ⁴

- $K_f' = K_f$ at pH = 0
- $K_f' = \alpha_{Y^{4-}} K_f$

- c) $K_f = \alpha_{Y^{4-}} \cdot K_f'$
- d) $K_f' = 1 / K_f$
- e) $K_f' = K_f^2$

5] It is advantageous to conduct EDTA titrations of metal ions in ⁵

- a) acidic pH's to assist metal ion hydrolysis
- b) basic pH's to prevent metal ion hydrolysis
- c) basic pH's to maximize Y^{4-} fraction
- d) basic pH's to minimize Y^{4-} fraction
- e) acidic pH's to maximize Y^{4-} fraction

6] What is K_f' for $SrEDTA^{2-}$ at pH 11? ⁶

7] The formal concentration of EDTA is 1.00 mM. What is the concentration of the Y^{4-} form at pH 4? ⁷

8] What is the conditional formation constant of $CaEDTA^{2-}$ at pH 10.00? ⁸

9] What is the conditional formation constant K_f' for CoY^{2-} at pH 10? ⁹

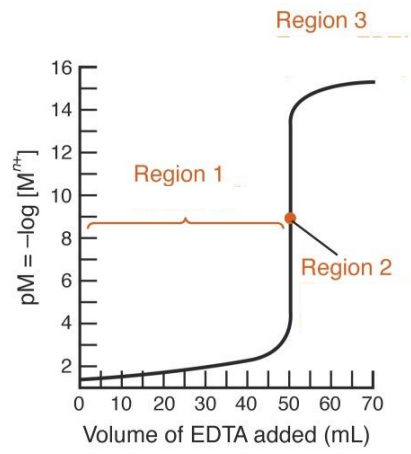
10] The fraction of free metal (α_m) in the following equilibrium can be expressed as: ¹⁰



11] Given that $\alpha_{Y^{4-}} = 3.8e-9$ at pH 4.00 & $\alpha_{Y^{4-}} = 1.9e-18$ at pH 1.00 what is the conditional formation constant for FeY^- at those pH's. $\log K_f = 25.1$ ¹¹

12] Calculate the concentrations of free Fe^{3+} in a 0.10 M FeY^- solution at pH 4.00 and 1.00. ¹²

13] Which of the three regions below is where moles of added EDTA equals moles of metal M^{n+} ? ¹³



14] For Ag^+ in the presence of NH_3 , $\log \beta_1 = 3.31$ and $\log \beta_2 = 7.23$. The fraction of free Ag^+ in solution can be calculated from: ¹⁴

a) $\alpha_{\text{Ag}^+} = 1 / \{1 + \beta_1[\text{NH}_3] + \beta_2[\text{NH}_3]^2\}$

b) $\alpha_{\text{Ag}^+} = 1 / \{1 + \beta_1[\text{NH}_3] + \beta_2[\text{NH}_3]\}$

c) $\alpha_{\text{Ag}^+} = 1 / \{1 + \beta_1[\text{NH}_3]^2 + \beta_2[\text{NH}_3]\}$

d) $\alpha_{\text{Ag}^+} = 1 / \{1 + \beta_1 + \beta_2\}$

e) $\alpha_{\text{Ag}^+} = \{1 + \beta_1[\text{NH}_3] + \beta_2[\text{NH}_3]^2\}$

15] Calculate the concentration of free Ca^{2+} when $[\text{Y}^{4-}] = 4.5\text{e-}3$ M, and $[\text{CaY}^{2-}] = 9.0\text{e-}3$, at pH 10. $K_f' = 1.8\text{e}10$. ¹⁵

16] Given that $K_f' = 1.00\text{e}+10$ for a complex AY^{2-} where (A = metal ion) at 0.010 M what is the concentration of free metal as pA? ¹⁶

17] Given $K_f' = 1.4\text{e}10$ for CaY^{2-} , what is pCa when 10.00 mL of $2.00\text{e-}3$ M of Ca^{2+} is added to 10.00 mL of $2.00\text{e-}3$ M EDTA? ¹⁷

18] A solution of 50.0-mL of 1.00×10^{-3} M $\text{NiCl}_2(\text{aq})$ is titrated with 1.00×10^{-3} M EDTA in a solution of 0.100 M NH_3 at pH 11.00. What is pNi if 25.0-mL of the titrant solution is added? Note that $\alpha_{\text{Ni}^{2+}} = 1.34 \times 10^{-4}$ at 0.100 M NH_3 . ¹⁸

19] What is K_f'' for the NiEDTA^{2-} complex in 0.100 M NH_3 at pH 11? ¹⁹

20] a) What is $[\text{NiEDTA}^{2-}]$ if 75.0-mL of titrant is added to the NiCl_2 solution in the above problem?

b) Which is true if 75.0-mL of 1.00×10^{-3} M EDTA titrant is added to the 50.0-mL of 1.00×10^{-3} M NiCl_2 solution in 0.1M NH_3 ? Assume equilibrium conditions. ²⁰

a) $[\text{Ni}^{2+}] = [\text{EDTA}]$

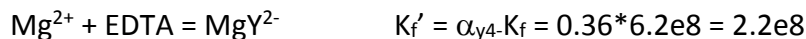
b) $[\text{NiEDTA}^{2-}] > [\text{EDTA}]$

c) $[\text{NiEDTA}^{2-}] = [\text{EDTA}]$

d) $[\text{Ni}^{2+}] > [\text{EDTA}]$

21] Given that $\beta_1 = 17$ for $\text{Ca}(\text{NH}_3)^{2+}$, calculate pCa. Assume that $[\text{NH}_3] = 0.100$ M and $[\text{Ca}(\text{NH}_3)^{2+}] = 1.00\text{e-}3$ M at pH 10.00. ²¹

22] A) Calculate the concentration of free Mg^{2+} in a solution of 50.0 mL of 0.0500 M Mg^{2+} when 5.00 mL of 0.0500 M EDTA is added at pH 10.00. ²²



B) When 50.0 mL of 0.0500 M EDTA is added.

C] When 51.00 of 0.0500 M EDTA is added.

23] Calculate pCa if 20.0 mL of 0.050 M of EDTA is added to 15.0 mL of 0.050 M Ca^{2+} at pH 9.0.
23

24] Calculate pCu for the titration curve for 50.00 mL of 0.0200 F Cu^{2+} at pH 5.00 when 0, 10.00, 25.00, 30.00 mL of 0.0400 M EDTA solution are added to the titration mixture. ²⁴

25] Calculate the conditional formation constant of $\text{Fe}^{\text{III}}(\text{Y})^-$ (where Y = EDTA) in presence of 0.0100 M NaOOCCH_3 at pH 7.00, if $C_{\text{Fe}^{3+}} = 1.00\text{e-}4$ M, and $[\text{EDTA}] = 1.50\text{e-}4$ M. ²⁵

26] a] Calculate the concentration of free Ag^+ for 0.010 F Ag^+ in 0.10 M NH_3 .

b] Calculate pAg when a 50.00-mL of 0.010 M(or F) Ag^+ is mixed with 75.00-mL of 0.010 M EDTA at pH 10.00 in 0.10 M NH_3 . ²⁶

27] 50 mL of 0.010 M Zn^{2+} is titrated with 0.010 M EDTA in 0.010 M NH_3 at pH 9.00. ²⁷

A] calculate K_f'' .

B] Calculate the pZn when 50.0 mL of 0.0100 M Zn^{2+} is added to 25.0 mL of 0.0100 M EDTA in 0.010 M NH_3 at pH 9.00.

C] Calculate the pZn when 50.0 mL of 0.0100 M Zn^{2+} is added to 50.0 mL of 0.0100 M EDTA in 0.010 M NH_3 at pH 9.00.

D] Calculate the pZn when 50.0 mL of 0.0100 M Zn^{2+} is added to 75.0 mL of 0.0100 M EDTA in 0.010 M NH_3 at pH 9.00.

Answers

¹ $3.7\text{e-}7$

² The fraction of EDTA in the Y^{4-} form.

³ B

⁴ $K_f' = \alpha_{\text{Y}^{4-}} \cdot K_f$

⁵ basic pH's to maximize Y^{4-} fraction

⁶ $K_f' = \alpha_{\text{Y}^{4-}} \cdot K_f = 0.85 \cdot 5.4\text{e}8 = 4.6\text{e}8$

⁷ $[\text{Y}^{4-}] = 3.8\text{e-}9 \cdot 1.00\text{e-}3 \text{ M} = 3.8\text{e-}12 \text{ M}$

$$^8 K_f' = 0.36 * 10^{10.69} = 1.8e-10$$

$$^9 K_f = 10^{16.31} = 2.04e16 \quad \text{At pH 10 } \alpha_{Y^{4-}} = 0.36 \text{ for EDTA } K_f' = 0.36 * 2.04e16 = 7.35e15$$

$$^{10} \alpha_m = \frac{1}{1 + \beta[L]}$$

$$^{11} K_f = [\text{FeY}^-] / [\text{Fe}^{3+}][\text{Y}^{4-}] \quad [\text{Y}^{4-}] = \alpha_{Y^{4-}}[\text{EDTA}]$$

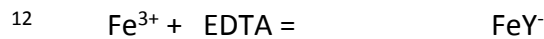
$$K_f = [\text{FeY}^-] / [\text{Fe}^{3+}]\alpha_{Y^{4-}}[\text{EDTA}]$$

$$K_f' = \alpha_{Y^{4-}} K_f = [\text{FeY}^-] / [\text{Fe}^{3+}][\text{EDTA}]$$

$$\text{Fe}^{3+} + \text{EDTA} = \text{FeY}^- \quad K_f' = \alpha_{Y^{4-}} K_f$$

$$\text{At pH 4.00} \quad K_f' = \alpha_{Y^{4-}} K_f = 3.8e-9 * 1.3e25 = 4.9e16$$

$$\text{At pH 1.00} \quad K_f' = 1.9e-18 * 1.3e25 = 2.5e7$$



$$0 \quad 0 \quad 0.10 \text{ M}$$

$$+x \quad +x \quad -x$$

$$0.10 - x / x^2 = K_f'$$

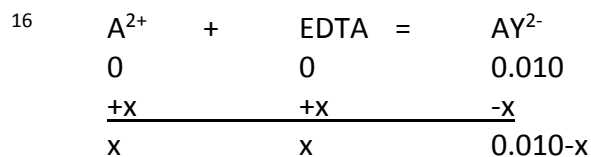
$$x = 1.4e-9 \text{ @ pH 4.00}$$

$$x = 6.3e-5 \text{ @ pH 1.00}$$

¹³ Region 2

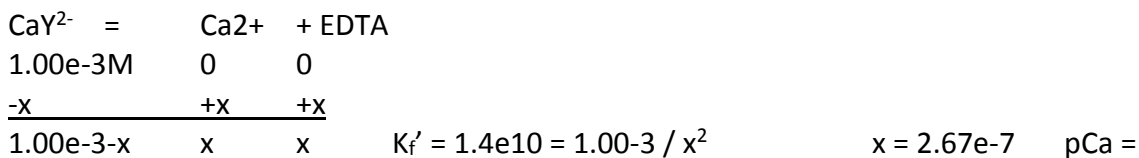
$$^{14} \alpha_{\text{Ag}^+} = 1 / \{1 + \beta_1[\text{NH}_3] + \beta_2[\text{NH}_3]^2\}$$

$$^{15} 1.8e10 = [9.0e-3] / [\text{Ca}^{2+}][4.5e-3] \quad [\text{Ca}^{2+}] = 1.11e-10$$



$$1.00e+10 = 0.010 - x / x^2 \cong 0.010 / x^2 \quad x = 1.00e-6 \quad \mathbf{pA = 6.00}$$

¹⁷ This is the equi. pt. $[CaY^{2-}] = 1.00e-3 \text{ M}$



6.57

¹⁸ Initial mol $Ni^{2+} = 50.0\text{-mL} * 1.00e-3 \text{ M} = 0.0500 \text{ mmol}$

Added mol EDTA

$$= 25.0\text{-mL} * 1.00e-3 \text{ M}$$

$$= 0.0250 \text{ mmol}$$

$$\text{Excess } Ni^{2+} = 0.0500 - 0.0250 \text{ mmol} = 0.0250 \text{ mmol}$$

$$C_{Ni^{2+}} = 0.0250 \text{ mmol} / 75.0\text{-mL}$$

$$= 3.33e-4 \text{ M}$$

$$\text{Free } [Ni^{2+}] = \alpha_{Ni^{2+}} C_{Ni^{2+}} = 1.34e-4 * 3.33e-4 = 4.47e-8 \text{ M}$$

pNi = 7.350

$$\supseteq K_f'' = \alpha_{Ni^{2+}} \alpha_{Y^{4-}} * K_f = 1.34e-4 * 0.85 * 10^{18.62} = \mathbf{4.7e14}$$

²⁰ Initial mol $Ni^{2+} = 50.0\text{-mL} * 1.00e-3 \text{ M} = 0.0500 \text{ mmol}$

$$\text{Added mol EDTA} = 75.0\text{-mL} * 1.00e-3 \text{ M} = 0.0750 \text{ mmol}$$

$$\mathbf{[NiEDTA] = 0.0500 \text{ mmol} / 125.0\text{-mL} = 4.00e-4 \text{ M}}$$

$$\text{Excess EDTA} = 0.0250 \text{ mmol} / 125.0\text{-mL} = 2.00e-4 \text{ M}$$

$$K_f'' = [NiEDTA] / C_{Ni} * [EDTA] = 4.00e-4 / C_{Ni} * 2.00e-4 = 4.7e14$$

$$C_{Ni} = 4.3e-15$$

$$[Ni^{2+}] = 1.34e-4 * 4.3e-15 = 5.8e-18 \text{ M}$$

$$pNi = 17.24$$

Therefore $[NiEDTA^{2-}] > [EDTA]$

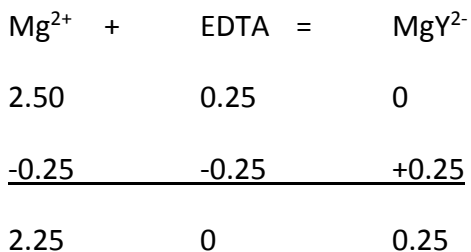
$$^{21} \text{ Need } \alpha_{Ca^{2+}} = 1 / (1 + \beta_1[NH_3]) \quad \text{from there: } [Ca^{2+}] = \alpha_{Ca^{2+}} 1.00e-3 \text{ M,}$$

$$\alpha_{Ca^{2+}} = 1 / (1 + \beta_1[NH_3]) = 1 / (1 + 17(0.100)) = 0.37$$

$$[Ca^{2+}] = \alpha_{Ca^{2+}} 1.00e-3 \text{ M} = 0.37e-3 \text{ M} \quad pCa = 3.43$$

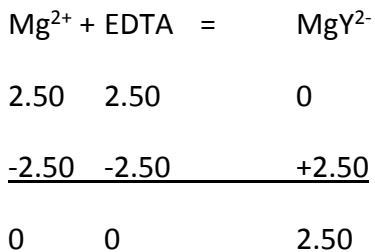
$$^{22} \text{ A) Initial } Mg^{2+} = 0.0500 \text{ M} * 50.0 \text{ mL} = 2.50 \text{ mmol}$$

$$\text{Added EDTA} = 0.0500 * 5.00 \text{ mL} = 0.25 \text{ mmol}$$

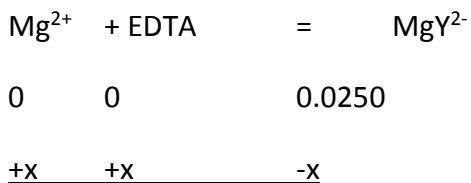


$$[Mg^{2+}] = 2.25 \text{ mmol} / 55.00 \text{ mL} = 0.0409 \text{ pMg} = 1.39$$

$$\text{B) added EDTA} = 0.0500 \text{ M} * 50.0 \text{ mL} = 2.50 \text{ mmol}$$



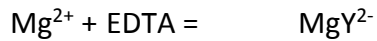
$$[Mg^{2+}] = 2.50 \text{ mmol} / 100 \text{ mL} = 0.0250 \text{ M}$$



$$0.0250 - x / x^2 = 2.2e8$$

$$x = 1.07e-5 \quad pMg = 4.97$$

C] added EDTA = 0.0500 M * 51.0 mL = 2.55 mmol



2.50 2.55 0

-2.50 -2.50 +2.50

0 0.05 2.50

$$[\text{MgY}^{2-}] = 2.50 \text{ mmol} / 101 \text{ mL} = 2.47\text{e-}2 \text{ M}$$

$$[\text{EDTA}] = 0.05 \text{ mmol} / 101 \text{ mL} = 4.95\text{e-}4$$

$$K_f' = [\text{MgY}^{2-}] / [\text{Mg}^{2+}][\text{EDTA}] = 2.47\text{e-}2 \text{ M} / [\text{Mg}^{2+}] * 4.95\text{e-}4$$

$$K_f' = 2.2\text{e}8$$

$$[\text{Mg}^{2+}] = 2.3\text{e-}7$$

$$\text{pMg} = 6.64$$

²³ mol EDTA = 20.0 mL * 0.050 M = 1.0 mmol

$$\text{mol Ca}^{2+} = 15.0 \text{ mL} * 0.050 \text{ M} = 0.75 \text{ mmol}$$

excess EDTA region where,

$$[\text{CaY}^{2-}] = 0.75 \text{ mmol} / 35.0 \text{ mL} = 2.1\text{e-}2 \text{ M}$$

$$[\text{EDTA}] = 0.25 \text{ mmol} / 35.0 \text{ mL} = 7.1\text{e-}3 \text{ M}$$

$$K_f = [\text{CaY}^{2-}] / [\text{Ca}^{2+}] * [\text{Y}^{4-}]$$

$$[\text{Y}^{4-}] = \alpha_{\text{Y}^{4-}} [\text{EDTA}]$$

$$K_f * \alpha_{\text{Y}^{4-}} = K_f' = [\text{CaY}^{2-}] / [\text{Ca}^{2+}] * [\text{EDTA}]$$

$$K_f = 4.9\text{e}10$$

$$K_f' = 5.4\text{e-}2 * 4.9\text{e}10 = 2.6\text{e}9$$

$$2.6\text{e}9 = 2.1\text{e-}2 \text{ M} / [\text{Ca}^{2+}] * 7.1\text{e-}3 \text{ M} \quad [\text{Ca}^{2+}] = 1.1\text{e-}9 \text{ M}$$

$$\text{pCa} = 8.94$$

²⁴ At 0.00 $[\text{Cu}^{2+}] = 0.020 \text{ M}$ **pCu = 1.70**

At 10.00 mL

Initial mols $\text{Cu}^{2+} = 0.0200 \text{ M} * 50.00 \text{ mL} = 1.00 \text{ mmols}$

Added mols EDTA = $0.040 \text{ M} * 10.00 \text{ mL} = 0.40 \text{ mmols}$

Excess $\text{Cu}^{2+} = 1.00 \text{ mmol} - 0.40 \text{ mmol} = 0.60 \text{ mmol}$

$[\text{Cu}^{2+}]_{\text{free}} = 0.60 \text{ mmol} / 60.00 \text{ mL} = 0.010 \text{ M}$

pCu = 2.00

At 25.00 mL

Initial mols $\text{Cu}^{2+} = 1.00 \text{ mmols}$

Added mols EDTA = $0.040 \text{ M} * 25.00 \text{ mL} = 1.0 \text{ mmols}$

This is the equivalence point therefore the formal concentration of CuEDTA is

$[\text{CuEDTA}] = 1.0 \text{ mmols} / 75.00 \text{ mL} = 1.3\text{e-}2 \text{ M}$

Now Calculate free Cu^{2+} :

$\text{Cu}^{2+} + \text{EDTA} \rightleftharpoons \text{CuEDTA}$

+x +x $1.3\text{e-}2 -x$

$K_f = 6.3\text{e}18$

@ pH 5.00

$\alpha_{Y4-} = 3.7\text{e-}7$

$K_f' = \alpha_{Y4-} K_f = 3.7\text{e-}7 * 6.3\text{e}18 = 2.33\text{e}12$

$1.3\text{e-}2 -x / x^2 = 2.33\text{e}12$

$1.3\text{e-}2 / x^2 \cong 2.33\text{e}12$

$x = 7.5\text{e-}8$

pCu = 7.12

At 30.00 mL

Initial mols Cu^{2+} = 1.00 mmols

Added mols EDTA = 0.0400 M * 30.00 mL = 1.20 mmols

Excess EDTA = 1.20 – 1.00 mmol = 0.20 mmol

$[\text{EDTA}]_{\text{excess}} = 0.20 \text{ mmol} / 80.00 \text{ mL} = 2.5\text{e-}3$

We now have the following equilibrium to consider:



+x 2.5e-3+x 1.3e-2 -x

$$(1.3\text{e-}2 - x) / (2.5\text{e-}3 + x) x = 2.33\text{e}12$$

$$(1.3\text{e-}2) / (2.5\text{e-}3) x \cong 2.33\text{e}12 \qquad x = 2.2\text{e-}12$$

pCu = 11.65

$$^{25} K_f(\text{Fe}^{\text{III}}(\text{OOCH}_3)_2^{2+}) = 10^{3.38} = 2.398\text{e}3$$

$$K_f(\text{Fe}^{\text{III}}(\text{OOCH}_3)_2^+) = 10^{7.1} = 1.26\text{e}7$$

$$K_f(\text{Fe}^{\text{III}}(\text{OOCH}_3)_3) = 10^{9.7} = 5.01\text{e}9$$

$$\begin{aligned} \alpha_{\text{Fe}^{3+}} &= 1 / \{1 + \beta_1[\text{CH}_3\text{OO}^-] + \beta_2[\text{CH}_3\text{OO}^-]^2 + \beta_3[\text{CH}_3\text{OO}^-]^3\} \\ &= 1 / \{1 + 2.398\text{e}3 [0.0100] + 1.26\text{e}7 [0.0100]^2 + 5.01\text{e}9 [0.0100]^3\} \\ &= 1 / \{1 + 2.398 + 1.26\text{e}3 + 5.01\text{e}3\} \\ &= 1 / 6.27\text{e}3 \\ &= 1.59\text{e-}4 \end{aligned}$$

$$\alpha_{\text{Y}^{4-}} @ \text{pH } 7.00 = 5.0\text{e-}4 \text{ (Table 13-1)}$$

$$K_f = 10^{25.1} = 1.3\text{e}25 \text{ (Table 13-2)}$$

$$K_f'' = \alpha_{\text{Fe}^{3+}}\alpha_{\text{Y}^{4-}}K_f = 1.59\text{e-}4 * 5.0\text{e-}4 * 1.3\text{e}25 = 1\text{e}18$$

²⁶ **a] See Appendix**

$$\beta_1 = 10^{3.31} = 2.04\text{e}3$$

$$\beta_2 = 10^{7.23} = 1.70\text{e}7$$

$$\alpha_{\text{Ag}^+} = 1 / (1 + \beta_1[\text{NH}_3] + \beta_2[\text{NH}_3]^2) = 1 / (1 + 2.04\text{e}3 * 0.100 + 1.70\text{e}7 * 0.100^2) = 5.88\text{e-}6$$

$$[\text{Ag}^+] = \alpha_{\text{Ag}^+} C_{\text{Ag}^+} = 5.88\text{e-}6 * 0.010 \text{ M} = 5.88\text{e-}8 \text{ M}$$

$$\mathbf{b) K_f'' = K_f \alpha_{\text{Ag}^+} \alpha_{\text{Y}4-} = 10^{7.32} * 5.88\text{e-}6 * 0.36 = 44.2}$$

$$\text{Initial mol Ag}^+ = 50.00\text{-mL} * 0.010 \text{ M} = 0.500 \text{ mmol}$$

$$\text{Added mol EDTA} = 75.00\text{-mL} * 0.010 \text{ M} = 0.750 \text{ mmol}$$

All Ag^+ is complexed with EDTA with leftover EDTA

$$[\text{AgY}^{3-}] = 0.500 \text{ mmol} / 125.00\text{-mL} = 4.00\text{e-}3 \text{ M}$$

$$[\text{EDTA}]_{\text{free}} = 0.250 \text{ mmol} / 125.00\text{-mL} = 2.00\text{e-}3 \text{ M}$$

$$K_f'' = [\text{AgY}^{3-}] / C_{\text{Ag}^+} [\text{EDTA}]$$

$$44.2 = 4.00\text{e-}3 \text{ M} / C_{\text{Ag}^+} 2.00\text{e-}3 \text{ M}$$

$$C_{\text{Ag}^+} = 4.52\text{e-}2$$

$$[\text{Ag}^+] = \alpha_{\text{Ag}^+} C_{\text{Ag}^+} = 5.88\text{e-}6 * 4.52\text{e-}2 \text{ M} = 2.66\text{e-}7 \text{ M}$$

$$\text{pAg} = 6.575$$

²⁷ A) Appendix I in your text has

$$\log \beta_1 = 2.18 \quad \beta_1 = 151$$

$$\log \beta_2 = 4.43 \quad \beta_2 = 2.69\text{e}4$$

$$\log \beta_3 = 6.74 \quad \beta_3 = 5.50\text{e}6$$

$$\log \beta_4 = 8.70 \quad \beta_4 = 5.01\text{e}8$$

$$\alpha_M = 1 / \{1 + \beta_1[L] + \beta_2[L]^2 + \dots + \beta_n[L]^n\}$$

$$\alpha_{\text{Zn}^{2+}} = 1 / \{1 + 151[0.010] + 2.69\text{e}4[0.010]^2 + 5.50\text{e}6[0.010]^3 + 5.01\text{e}8[0.010]^4\}$$

$$\alpha_{\text{Zn}^{2+}} = 1 / \{1 + 1.51 + 2.69 + 550.0 + 5010.0\}$$

$$= 1.79\text{e-}4$$

$$K_f = 3.2\text{e}16 \quad \text{Table 13-2}$$

$$\alpha_{\text{Y}4-} = 5.4\text{e-}2 \quad \text{Table 13-1}$$

$$K_f'' = K_f \alpha_{Zn^{2+}} \alpha_{Y^{4-}} = 3.2e16 * 5.4e-2 * 1.79e-4 = 3.1e11$$

$$B) \text{ Initial } Zn^{2+} = 50.0 \text{ mL} * 0.0100 \text{ M} = 0.500 \text{ mmol}$$

$$\text{Added EDTA} = 25.0 \text{ mL} * 0.0100 \text{ M} = 0.250 \text{ mmol}$$

$$\text{Excess } Zn^{2+} = 0.500 - 0.250 = 0.250 \text{ mmol}$$

$$C_{Zn^{2+}} = 0.250 \text{ mmol} / 75.0 \text{ mL} = 3.33e-3 \text{ M}$$

$$[Zn^{2+}] = \alpha_{Zn^{2+}} C_{Zn^{2+}} = 1.79e-4 * 3.33e-3 \text{ M}$$

$$pZn = 6.225$$

$$C) \text{ Initial } Zn^{2+} = 50.0 \text{ mL} * 0.0100 \text{ M} = 0.500 \text{ mmol}$$

$$\text{Added EDTA} = 50.0 \text{ mL} * 0.0100 \text{ M} = 0.500 \text{ mmol}$$

$$\text{Initial } Zn^{2+} = \text{Added EDTA} \therefore \text{eq. pt.}$$

$$\text{Initial } [ZnY^{2-}] = 0.500 \text{ mmol} / 100.0 \text{ mL} = 5.00e-3 \text{ M}$$

$$ZnY^{2-} = C_{Zn^{2+}} + EDTA$$

$$5.00e-3 \quad 0 \quad 0$$

$$-x \quad +x \quad +x$$

$$K_f'' = 3.1e11 = (5.00e-3 - x) / x^2$$

$$x = C_{Zn^{2+}}$$

$$x = 1.27e-7 \text{ M}$$

$$[Zn^{2+}] = \alpha_{Zn^{2+}} C_{Zn^{2+}} = 1.79e-4 * 1.27e-7 \text{ M}$$

$$[Zn^{2+}] = 2.27e-11 \text{ M}$$

$$pZn = 10.64$$

$$D) \text{ Initial } Zn^{2+} = 50.0 \text{ mL} * 0.0100 \text{ M} = 0.500 \text{ mmol}$$

$$\text{Added EDTA} = 75.0 \text{ mL} * 0.0100 \text{ M} = 0.750 \text{ mmol}$$

$$\text{Excess EDTA} = 0.250 \text{ mmol}$$

$$[ZnY^{2-}] = 0.500 \text{ mmol} / 125.0 \text{ mL} = 4.00e-3$$

$$[\text{EDTA}] = 0.250 \text{ mmol} / 125.0 \text{ mL} = 2.00\text{e-}3 \text{ M}$$

$$K_f'' = 3.1\text{e}11 = [\text{ZnY}^{2-}] / C_{\text{Zn}^{2+}} * [\text{EDTA}]$$

$$3.1\text{e}11 = 4.00\text{e-}3 / C_{\text{Zn}^{2+}} * 2.00\text{e-}3$$

$$C_{\text{Zn}^{2+}} = 6.45\text{e-}12$$

$$[\text{Zn}^{2+}] = \alpha_{\text{Zn}^{2+}} C_{\text{Zn}^{2+}} = 1.79\text{e-}4 * 6.45\text{e-}12\text{M} = 1.15\text{e-}15$$

$$p\text{Zn} = 14.94$$