## Homework 1

## MATH 420

Please email me your homework as a pdf file
All work must be shown clearly. You must justify all your answers.

1. Verify that

$$
(\sqrt{2}-i)-i(1-i \sqrt{2})=-2 i
$$

2. Solve the quadratic equation $z^{2}+z+1=0$.
3. Reduce the following

$$
\frac{1+i 2}{3-i 4}+\frac{2-i}{5 i}
$$

4. Use properties of conjugates and modulus to show that

$$
|(2 \bar{z}+5)(\sqrt{2}-i)|=\sqrt{3}|2 z+5|
$$

5. Describe clearly the geometric object determined by the condition

$$
|2 \bar{z}+i|=4
$$

