## Homework 1

## **MATH 420**

Please email me your homework as a pdf file All work must be shown clearly. You must justify all your answers.

1. Verify that

$$(\sqrt{2} - i) - i(1 - i\sqrt{2}) = -2i$$

- 2. Solve the quadratic equation  $z^2 + z + 1 = 0$ .
- 3. Reduce the following

$$\frac{1+i2}{3-i4} + \frac{2-i}{5i}$$

4. Use properties of conjugates and modulus to show that

$$|(2\overline{z}+5)(\sqrt{2}-i)| = \sqrt{3}|2z+5|$$

5. Describe clearly the geometric object determined by the condition

$$|2\overline{z} + i| = 4$$