$\qquad$

This test is closed book and closed notes. Calculators of any kind are not allowed. You must clearly show your work to receive credit. Unless otherwise stated, you do not need to simplify your answer.

1. Find $\int \sin ^{2} x \cos ^{3} x d x$. (11 points)
2. Find $\int \tan ^{3} x \sec ^{5} x d x$. (11 points)
3. Find $\int \frac{1}{\sqrt{9+x^{2}}} d x$. (11 points)
4. Find $\int \frac{1}{x(x-1)^{2}} d x$. (11 points)
5. Find $\int \frac{x-1}{x+1} d x$. (11 points)
6. Use Simpson's rule to estimate $\int_{0}^{4} \sin (\pi x) d x$ using $n=4$ subintervals. (11 points)
7. Determine whether $\int_{8}^{\infty} \frac{1}{(x+1)^{3 / 2}} d x$ diverges or converges. If it converges, find the value of the integral. (11 points)
8. Solve the differential equation $y^{\prime}=\cos ^{2} y$ subject to the initial condition $y(0)=\pi / 4$. (11 points)
9. Find a recurrence relation for the sequence $\left\{a_{n}\right\}_{n=0}^{\infty}=\{1,2,4,8,16, \ldots\}$. (11 points)
