

```

/* SAS program for a factorial experiment */
/* with two random factors, using PROC GLM. */
/* Data are from the text, Example 17.2, p. */
/* 987. Response is amount of calcium */
/* measured in a standardized preparation */
/* containing 10 mg calcium. Random factor */
/* ASSAY is assay method, random factor LAB */
/* is laboratory. */

options nocenter ls=72;
data;
  input y assay lab @@;
cards;
10.9 1 1 10.9 1 1 10.5 1 2 9.8 1 2 9.7 1 3 10.0 1 3
11.3 2 1 11.7 2 1 9.4 2 2 10.2 2 2 8.8 2 3 9.2 2 3
11.8 3 1 11.2 3 1 10.0 3 2 10.7 3 2 10.4 3 3 10.7 3 3
;
proc glm;
  class assay lab;
  model y=lab assay lab*assay;
  random lab assay lab*assay / test;
run;

```

The GLM Procedure

Class Level Information

Class	Levels	Values
assay	3	1 2 3
lab	3	1 2 3

Number of observations 18  
 Dependent Variable: y

Source	DF	Sum of Squares	Mean Square	F Value
Model	8	10.76000000	1.34500000	9.76
Error	9	1.24000000	0.13777778	
Corrected Total	17	12.00000000		

Source	Pr > F
Model	0.0013

Error  
 Corrected Total

R-Square	Coeff Var	Root MSE	y Mean
0.896667	3.569080	0.371184	10.40000

Source	DF	Type I SS	Mean Square	F Value
lab	2	7.56000000	3.78000000	27.44
assay	2	1.56000000	0.78000000	5.66
assay*lab	4	1.64000000	0.41000000	2.98

Source	Pr > F
lab	0.0001
assay	0.0256
assay*lab	0.0803

Source	DF	Type III SS	Mean Square	F Value
lab	2	7.56000000	3.78000000	27.44
assay	2	1.56000000	0.78000000	5.66
assay*lab	4	1.64000000	0.41000000	2.98

Source	Pr > F
lab	0.0001
assay	0.0256
assay*lab	0.0803

Source	Type III Expected Mean Square
lab	$\text{Var}(\text{Error}) + 2 \text{Var}(\text{assay*lab}) + 6 \text{Var}(\text{lab})$
assay	$\text{Var}(\text{Error}) + 2 \text{Var}(\text{assay*lab}) + 6 \text{Var}(\text{assay})$
assay*lab	$\text{Var}(\text{Error}) + 2 \text{Var}(\text{assay*lab})$

Tests of Hypotheses for Random Model Analysis of Variance

Dependent Variable: y

Source	DF	Type III SS	Mean Square	F Value
lab	2	7.560000	3.780000	9.22
assay	2	1.560000	0.780000	1.90
Error: MS(assay*lab)	4	1.640000	0.410000	

Source	Pr > F
lab	0.0318
assay	0.2627

Error: MS(assay\*lab)

Source	DF	Type III SS	Mean Square	F Value
assay*lab	4	1.640000	0.410000	2.98
Error: MS(Error)	9	1.240000	0.137778	

Source	Pr > F
assay*lab	0.0803

Error: MS(Error)