

What if you fit the wrong model?

$$y_i = a_0 + a_1 x_{i1} + a_2 x_{i2} + a_3 x_{i2}^2 + \epsilon_i$$

we fit

$$\hat{y}_i = \hat{b}_0 + \hat{b}_1 x_{i1} + \hat{b}_2 x_{i2} \quad \text{no } x_{i2}^2$$

$$\epsilon_i = y_i - \hat{y}_i = (a_0 - \hat{b}_0) + (a_1 - \hat{b}_1)x_{i1} + (a_2 - \hat{b}_2)x_{i2}$$

instead

$$+ a_3 x_{i2}^2 + \epsilon_i$$

$$\epsilon_i + \hat{b}_2 x_{i2} = (a_0 - \hat{b}_0) + (a_1 - \hat{b}_1)x_{i1} + a_2 x_{i2} + a_3 x_{i2}^2 + \epsilon_i$$