Flatland in flames: a two-dimensional canopy fire propagation model

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Non-specialist summary:

Canopy fire modeling is based largely upon the use of canopy bulk density, a three-dimensional crown measure, as a fuel metric. We propose and test a model that relies on a two-dimensional crown measure, which is simpler to conceptualize and easier to obtain remotely. We compare the model with its three-dimensional equivalent, with two contemporary fuel inputs methods. We find that the alternative fuel metric provides statistically equivalent modeled outputs of canopy fire propagation 2626 FIA plots.

Abstract:

Canopy bulk density (CBD) is widely used as metric for quantifying the fuel available for combustion in canopy fire and as an input to Van Wagner’s (1977) model for estimating the critical rate of spread necessary to sustain active canopy fire. We propose a modification of Van Wagner’s approach to use foliar biomass per unit area (FBA) as the fuel input. Unlike CBD, FBA does not require incorporation of the vertical distribution of the fuel, so it is readily measurable (and estimable) by foresters, tree physiologists and fire managers. The new model provides a more consistent explanation for Van Wagner’s original observations. We test our modified model for equivalence to the original Van Wagner model, incorporating two contemporary techniques for calculating CBD. We find that the modified model is equivalent to the original model using the CBD method incorporated into the Fire and Fuels Extension to the Forest Vegetation Simulator, but not the CBD method of Cruz et al. (2003). Although equivalent (at $\alpha = .10$, $N = 2626$) the FBA input produced a mean difference of 0.010 ms$^{-1}$ less for the critical rate of spread necessary to sustain canopy fire. The adoption of FBA as a fuel input may allow for consistent fuel quantifications that are less influenced by the highly varied canopy structure.
of forested stands than CBD, and could facilitate remotely sensed canopy fuel quantification.

**Introduction:**

Canopy fire is a challenge for the accurate modeling of fire spread because quantification of the canopy fuel stratum is difficult (Cruz et al. 2003, Keane et al. 2005). Particular difficulty arises because canopy fires can exist in either ‘passive’ or ‘active’ modes. In passive canopy fires, individual trees or groups of individuals ignite and burn from the bottom to the top of the crown, resulting in mixed impacts on the environment (Ryan and Noste 1983). In active canopy fires the combustion propagates as a solid wall of flame through a landscape filled with trees, in conjunction with a surface fire (Van Wagner 1977). In addition, this combination of active canopy and surface fire often burns at high intensity having significant impact on soils, vegetation, and wildlife habitat (Grier 1975, Ryan and Noste 1983, Romme 1995, Haggard and Gaines 2001). Such fires may exhibit flame lengths exceeding 30-m with rates of spread exceeding 50 m min\(^{-1}\) (Stocks et al. 2004). Active canopy fire also poses great risk to fire personnel, the public, and private property (Scott 1998, Clark et al. 1999, Scott and Reinhardt 2001).

For these reasons, fire managers seek to implement preventative treatment of forested landscapes capable of sustaining active canopy fires (Hof and Omi 2003, Scott 2003, Peterson et al. 2005). They also wish to predict and understand the behavior of these fires (Stocks et al. 2004). Such applications require knowledge of the minimal conditions required to sustain a canopy fire to support mitigation treatments and assessment of hazard to fire personnel during active fires.
Most fire planning tools and spatially explicit fire models depend upon Van Wagner’s (1977) model (we refer to this model as VWcbd) to characterize the minimum conditions necessary to sustain active canopy fire (Keane et al. 2000, Scott and Reinhardt 2001, Finney et al. 2003, Reinhardt and Crookston 2003, Finney 2004). VWcbd relies on a three-dimensional metric of available canopy fuel for combustion called canopy bulk density (CBD), which other research has attempted to quantify (Keane et al. 2000, Fule et al. 2001, Hummel and Agee 2003, Riano et al. 2003, Gray and Reinhardt 2003, Perry et al. 2004, Riano et al. 2004, Falkowski et al. 2005, Peterson et al. 2005, Keane et al. 2005). However, the dominant sources of information, and frameworks within which fire management decisions are made, are inherently two dimensional.

The ability to field test, calibrate, refine, or even observe the efficacy of the VWcbd estimates has been limited mostly because of the inherent difficulties of obtaining the three-dimensional CBD input. Scott and Reinhardt (2005) report nearly 1000 person-hours required to physically measure several canopy biomass variables (including their vertical distribution) to calculate canopy fuel CBD for a single 10m radius plot. This expense to physically measure the volume space used in CBD calculations has made it difficult to assess the utility of the model as put forth by Van Wagner (1977) (Keane et al. 2005).

We develop VWfba, a modified version of VWcbd, that uses foliar biomass per unit area (FBA) as a fuel input. Use of FBA may allow for consistent fuel quantifications that are less influenced than CBD by highly varied canopy structure common in forested stands. We compare VWfba with the existing VWcbd, using two different CBD estimation methods, to determine if FBA can be used with confidence in existing fire modeling applications with minor modification. The relationship of FBA to traditional
forest mensuration, forest physiology, and remote sensing variables should make canopy
fuel estimates more consistent and readily attainable for forest manager concerned with
canopy fire propagation and fuels management.

**Crown fire defined:**

Van Wagner (1977) described a conceptual canopy fire model using “a stationary wall
of flame with a conveyor belt carrying fuel into the flame”. The conveyor belt must
maintain a rate greater than minimum critical rate of spread (cROS) in order to deliver a
sufficient quantity of combustible fuel per unit time to maintain the wall of flame in the
canopy space (Van Wagner 1977).

Van Wagner modeled canopy fire interactions for fuel, flame front rate of spread, and
the *minimum* fireline intensity necessary to maintain canopy fire in a fashion similar to
Byram’s (1959) index. This surface fire index relates fireline intensity, the rate of spread of
a flame front, and the quantity of *combusted* fuel (Byram 1959, Scott and Reinhardt 2001).

By representing the flame front as a line moving at some rate across a plane of
homogenously distributed fuel mass (multiplied by a constant heat yield) the result is a
fireline intensity that is the product of the rate of flame movement and the homogeneous
fuel (Byram 1959). Like Byram’s (1959) index, the VWcbd assumes a homogeneously
distributed fuelbed, albeit through a volume rather than across an area (Van Wagner 1977).
The assumption of a homogeneous fuel bed with a constant heat yield per unit of fuel
makes VWcbd identical to Byram’s (1959) index in form.

The Van Wagner (1977) model differs only in form by its calibration to the *minimal*
conditions necessary for active canopy fire to persist. Van Wagner assumed that the fuel
present in a stand would have a constant heat of ignition (per unit mass), and thus avoided
the necessity of calculating the energy in the propagating heat flux. This changed the crucial element to a simple argument that relates only the critical quantity of fuel consumed per unit time required for flame maintenance, divided by the available fuel quantity (Eq. 1). The result of this equation is the critical rate of spread (cROS, represented by ‘\( R_0 \)’ in Eq. 1) required for the fire to consume the available fuel (‘\( d \)’) such that the critical mass flow rate (‘\( S_o \)’) is satisfied.

\[
R_0 = \frac{S_o}{d} \quad (Van \ Wagner \ 1977)
\]  

Where:  
\( R_0 \): cROS for active canopy fire (m s\(^{-1}\))  
\( S_o \): critical mass flow rate for canopy fire, (0.05 kg m\(^{-2}\) s\(^{-1}\))  
\( d \): foliar (canopy) bulk density (kg m\(^{-3}\))

Van Wagner’s definition of canopy fire as a wall of continuous flame from bottom to top of the canopy must be met to satisfy the implicit assumption that canopy fire has initiated (Van Wagner 1977; Scott and Reinhardt 2001). The use of a single value to represent a distribution of fuel through the canopy space removes any influence that the vertical distribution of fuel may have upon canopy fire, requiring a second assumption that horizontal canopy fire propagation occurs regardless of the vertical distribution of the fuel. The quotient resulting from the division of the available fuel by volume (the definition of CBD) is simply a fraction of the total fuel load (the sum of which is still available for combustion) and does not relate to the effect that the vertical distribution may (or may not) have on canopy fire.

A properly calibrated model that uses a fuel metric with no vertical distribution component does not preclude the use of vertical distribution as a parameter in the model.
The fuel input to such a model would be useable at a range of scales depending only upon the method used to calculate the available canopy fuel. We assume that the Van Wagner (1977) model appropriately relates the basic properties necessary to describe the lower boundary conditions required for active canopy fire combustion. (Namely, that an active canopy fire spreading between two points on the landscape must consume a minimum quantity of fuel per unit time in order to persist as a canopy fire.) The quantification of fuel is vital to a model of the combustion process. However, we argue that the quantification need not incorporate the vertical distribution into the fuel metric as traditional canopy fuel methodologies have done. We use Van Wagner’s (1977) published data to recalibrate the model for use with FBA in place of the standard CBD input. The VWcbd and the VWfba models are applied to a region-wide non-spatial FIA database and an equivalence test is used to compare the estimates of cROS from the VWcbd and VWfba models.

**Methods**

In this section we introduce two methods used to calculate the fuel input necessary for VWcbd. We compared only the Fire and Fuels Extension to the Forest Vegetation System (FFE) (Reinhardt and Crookston 2003) and Cruz et al. (2003) methods because they represent the two distinct approaches to estimating CBD. We then modify the existing VWcbd for the use of foliar biomass to create the VWfba model. Finally, we introduce our data and the statistical methods used to test the equivalence of the VWcbd and VWfba.
Summary of CBD methods:


When applied to a stand inventory list, FFE calculates the foliar biomass assuming a constant density of foliar biomass through the length of the individual tree-crown space. FFE calculates the amount of biomass contained in every vertical 0.3048 meter (1-foot) of the volume space for each tree (Scott and Reinhardt 2001). Finally, the foliar biomass for all individuals in the stand is summed within each vertical 0.3048 meter above the ground and is plotted (see Fig. 1). This represents stand biomass (kg m$^{-2}$) distributed by height above ground (m), as a sum of all individual trees (i.e. vertical distribution of foliage within the canopy space) (Sando and Wick 1972).

FFE calculates the maximum 0.3048 m (1 ft) increment of a 3.96 m (13-foot) running mean applied to the vertical profile of foliar biomass (see Fig. 1) (Reinhardt and Crookston 2003). This produces an effective CBD value that differs from the traditional CBD definition (Scott and Reinhardt 2001). Effective CBD provides a value that is the maximum of a running average (Fig 1) and represents the greatest average fuel value, presumed to be the least resistant stratum for canopy fire propagation through a stand (Scott and Reinhardt 2001). Despite the lack of direct correspondence to the CBD definition, effective CBD is frequently used as input to VWcbd.
Cruz et al. (2003) sum the foliar biomass for all trees in a stand and divide this by the product of the average vertical crown length multiplied by the area of the stand. Biomass is assumed to have equal distribution through the volume of the canopy. This method appears to be similar to the method used by Van Wagner (1977) for calculation of experimental fuels data. We refer to this method as the “Cruz” method for the remainder of this paper.

Modification of Van Wagner’s (1977) Model

We modify VWcbd (Eq. 2a) (Van Wagner 1977) by altering the mass flow rate ($S_o$, equation 2a), which represents the minimum quantity of fuel required to be combusted per unit time to sustain canopy fire propagation. To determine $S_o$, Van Wagner identified forested stands for canopy fire experimentation and recorded stand information including stems per hectare, basal area, tree height, height to crown base, and biomass per unit area (Table 1). The stands were then ignited with three out of four fires judged to burn as active canopy fires by Van Wagner (1977) (Table 1).

\[
R_o = \frac{S_o}{d} = \frac{0.05(kgm^{-2}s^{-1})}{d(kgm^{-3})} \quad \text{(Van Wagner 1977)} \quad (2a)
\]

\[
S_o = R_o \cdot d \quad \text{(2b)}
\]

$R_o$ is the critical minimum rate of spread for active canopy fire

$S_o$ is the critical mass flow rate for solid crown flame

$d$ is the canopy bulk density

Van Wagner (1977) used one stand (‘R1’ in Table 1), considered ‘an incipient’ active canopy fire, for model calibration. The observed rate of spread of fire in stand ‘R1’ was multiplied by CBD to determine the required mass flow ($S_o$ in Eq. 2b)(Van Wagner 1977).
It was apparent that this resulting value was less than necessary for active canopy fire so Van Wagner set $S_0$ at a constant value slightly greater ($0.05 \text{ kg m}^{-2} \text{s}^{-1}$) (VanWagner 1977). This established the minimum mass flow value necessary because a slower fuel consumption rate would result in fire behavior similar to the incipient canopy fire behavior of ‘R1’ (Van Wagner 1977).

For VWfba, we divide Van Wagner’s value of $S_0 = 0.05 \text{ kg m}^{-2} \text{s}^{-1}$ by the CBD for stand ‘R1’ ($0.23 \text{ kg m}^{-3}$) (Eq. 3a). The result is a cROS of $0.217 \text{ m s}^{-1}$ for stand ‘R1’. The cROS is multiplied by the FBA (foliar biomass per unit area, Table 1) of stand ‘R1’ resulting in a product of $0.39 \text{ kg m}^{-2} \text{s}^{-1}$ (Eq. 3b) giving the predictive equivalent to Van Wagner’s published value using CBD of $S_0 = 0.05 \text{ kg m}^{-2} \text{s}^{-1}$ (Eq. 3c).

\begin{align*}
0.05(\text{kg m}^{-2}\text{s}^{-1}) &\div 0.23(\text{kg m}^{-3}) = 0.217(\text{m s}^{-1}) \quad \text{(3a)} \\
0.217(\text{m s}^{-1}) &\times 1.80(\text{kg m}^{-2}) = 0.39(\text{kg m}^{-1}\text{s}^{-1}) \quad \text{(3b)} \\
\frac{0.05(\text{kg m}^{-2}\text{s}^{-1})}{0.23(\text{kg m}^{-3})} &\times 0.217(\text{m s}^{-1}) = \frac{0.39(\text{kg m}^{-1}\text{s}^{-1})}{1.80(\text{kg m}^{-2})} \quad \text{(3c)}
\end{align*}

The final form of the VWfba model is then:

\begin{equation}
R_o(\text{m s}^{-1}) = \frac{0.39(\text{kg m}^{-1}\text{s}^{-1})}{d(\text{kg m}^{-2})} \quad \text{(4)}
\end{equation}

After recalibration of $S_0$, the VWfba model was applied to the rest of the data provided by Van Wagner (1977) (Fig. 2). With exception of the calibration fire ‘R1’, all of these fires were observed canopy fires. A satisfactory model will have a predicted cROS that is exceeded by the observed rate of spread. Inputs for these predictions were taken from Van...
Wagner’s published data. The method of cbd estimation for input to the original VW model is unspecified. The published foliar biomass per unit ground area for these stands is used as FBA input to the VWfba model. The VWfba and VWcbd (where FBA and cbd inputs are provided in Van Wagner (1977)) models provide comparable predictions of cROS (Fig. 2). Additionally, VWfba identifies stand “GLB Active” as exceeding the cROS, and correctly classifies it as an active canopy fire, whilst VWcbd does not (Fig. 2).

Sample data

We use a database of 2626 Forest Inventory and Analysis (FIA) plots collected from the Inland Northwest region of the United States (Gillespie 1999, UIFBL 2006). FIA routinely collects data on trees, saplings, and seedlings at each plot; however, we selected only trees at least 7.56 cm (3”) in diameter at breast height (1.37 meters) (USDA Forest Service 1990). Each of the 40,000 tree records in this database include the variables of tree diameter, height, percent live crown ratio, species, and the tree expansion factor (number of trees per hectare that record represents) and plot level variables (e.g. elevation, habitat type, aspect, and slope.

Statistical analysis

Model validation is poorly served by traditional frequentist null hypothesis significance testing (NHST), because NHST requires that the null hypothesis be stated such that the two models are not significantly different (Wellek 2003). The ability to demonstrate similarity rather than difference based on probability arises by changing the null hypothesis from one of similarity; to one stating that dissimilarity exists, and is called equivalence testing (Wellek 2003; Robinson and Froese 2004). Though the biomedical industry has long used equivalence tests to show that two samples are statistically similar, equivalence tests have
not been widely applied to ecological modeling (Wellek 2003, Robinson and Froese 2004). Robinson and Froese (2004) use equivalence tests to validate model predictions of the diameter growth model contained within the Forest Vegetation Simulator.

This test requires that a region of indifference ($\varepsilon$), or a range of difference that is of negligible concern, be established (Robinson and Froese 2004). That is, a range of difference between sample metrics that is insignificant in practical application (Wellek 2003). After establishing a region of indifference, two separate trials of a one sided t-test on the difference between samples is carried out, one for differences greater than the test statistic, and one trial for differences less than the test statistic (Robinson and Froese 2004). This method is called a ‘two-one-sided t-test’ (TOST) and like a regular t-test, this test gains power as the sample size increases (Robinson and Froese 2004).

The null hypothesis of dissimilarity is rejected if the range of indifference overlaps into the rejection region for a one-tailed 95% confidence interval of the mean of the differences ($x_a - x_b = x_{diff}$) (Robinson and Froese 2004). The mathematics behind equivalence testing do not make p-values practical, so we use both a strict (small) and liberal (large) range of indifference to bracket our confidence in the hypothesis test (Wellek 2003).

These ranges of indifference bracket our confidence based not on probability, but on a judgment of how large the difference could be for the models to still be considered equivalent. In this paper, we choose a strict range of indifference such that $|\bar{x}_{diff} \pm \varepsilon| < 0.138 \text{ m s}^{-1}$ ($\pm 0.50 \text{ kph}$) for cROS, while the liberal range of indifference was established such $|\bar{x}_{diff} \pm \varepsilon| < 0.278 \text{ m s}^{-1}$ ($\pm 1.0 \text{ kph}$). The values were chosen as being insignificant ranges of difference from both a management and a modeling standpoint. We use a one
sided type I error rate of 5% (\(\alpha = .05\)), which translates to two times a one-sided \(\alpha\) (2 x .05 = .10) for our TOST test of equivalence.

Results

Our data exhibit light tails, relative to the normal distribution, however our large sample size lends resistance to departures from normality (Ramsey and Schafer 2002). To verify that outliers were not affecting the results we removed obvious outliers and reran the TOST. In each comparison of models, removing the outliers made the minimum region of indifference smaller. Hence, the null hypothesis was more clearly rejected with the outliers removed in each comparison and we present our results with all data represented.

The mean of the differences between cROS for FIA plots using VWcbd-FFE and VWfba is only 0.010 ms\(^{-1}\) (Table 2). Despite a comparatively large standard deviation the null hypothesis of dissimilarity is rejected. The sum of the minimum range of indifference and the mean of the difference (0.010 ± 0.027 ms\(^{-1}\)) is substantially less than the conservative range of indifference lending strong evidence (in lieu of a p-value) that the rejection of the null hypothesis is justified (Table 2).

These same patterns are repeated for the comparison of VWcbd-Cruz and VWcbd-FFE, though the mean of the difference is larger than the previous comparison (0.050 ms\(^{-1}\)) (Table 2). Again, the sum of the difference and the minimum range of indifference (0.050 ± 0.066 ms\(^{-1}\)) is well within the predefined conservative range of indifference leading to a comfortable rejection of the null hypothesis. In the final comparison between VWcbd-Cruz and VWfba the mean of differences is larger than any of the previous comparisons (0.060 ms\(^{-1}\)) (Table 2). The sum of this large bias between the models and corresponding large minimum region of indifference (0.060 ± 0.086 ms\(^{-1}\)) does not allow a rejection of the null
hypothesis of dissimilarity under the conservative scenario, though it is still rejected at the liberal range. In all but one of these comparisons we reject the null hypothesis of dissimilarity.

**Discussion**

The VWfba provides the lowest estimate of cROS between these three methods. These differences, 0.010 ms$^{-1}$ and 0.060 ms$^{-1}$, are interpreted to mean that on average the VWfba model estimates the cROS necessary to sustain canopy fire to be less than the cROS predicted by the VWcbd-FFE and VWcbd-Cruz respectively. This result is likely due the VWfba utilization of all available fuel and not some fraction of the available fuel which means that the cROS does not need to be as high as the case where less fuel is available.

The VWcbd and VWfba estimates for the regional FIA data (n=2676) are equivalent to one another well within acceptable ranges of indifference established for these tests. We demonstrate that VWfba is equivalent to VWcbd in the Inland Northwest when the sampling design of FIA is followed and the data used to describe a 0.40 hectare (1 acre) stand. Based on our analysis of comprehensive FIA data, we conclude that the use of VWfba is a reasonable alternative to VWcbd, in particular when compared to VWcbd-ffe.

Like CBD estimates, FBA is limited by the accuracy of the technologies used to estimate foliar biomass (total available fuel). However, CBD methods have the added difficulty of measuring the necessary volume. The ability to field test, calibrate, refine, or even observe the efficacy of the VWcbd estimates has been limited mostly because of the complex, more difficult measurement of the CBD input.

In summary, the adoption of VWfba may allow for consistent fuel quantifications that are less influenced by the highly varied canopy structure of forested stands than CBD.
Furthermore, data collection for VWfba should be much cheaper, and easier over large scales, if it can be related to remotely sensed measurements. The VWfba recalibration of Van Wagner’s (1977) model provides statistically equivalent estimates and is consistent with the original field observations of Van Wagner (1977).

The VWfba model proposed here only quantifies the fuel conditions necessary to sustain canopy fire between two points on the landscape with the intention of matching the performance of the original Van Wagner (1977) model. This model does not require knowledge about the vertical distribution of fuel, only that enough fuel exists between two points to sustain canopy fire. Future work with the VWfba model may require a coefficient to describe vertical distribution or a number of other parameters, but these coefficients will be independent of the combustible biomass estimate. This approach leads to a more subtle refinement of the model output independent of the quantity of fuel that is truly available to the advancing canopy fire.

The VWfba model should next be applied to a variety of case studies where estimates of foliar biomass can be obtained for observed canopy fires. An example of this sort of validation could be the acquisition of LANDSAT imagery over an area subsequent to a canopy fire. Using estimates of foliar biomass derived from leaf area index (LAI) and specific leaf area (SLA), the resulting VWfba prediction could be compared to fire behavior observations from that fire. This type of field validation removes the necessity of estimating the probable fire spread direction and then placing fuel sampling personnel directly in the path of impending canopy fires, allowing the required fire observations to be conducted from a safe distance. Given the lack of literature suggesting that the use of VWcbd adequately provides estimates of the cROS threshold we would not necessarily
expect the VWfba model to accurately estimate cROS in these field trials, but we would
expect it to perform as well as the VWcbd model, if reliable CBD data could be collected
for comparison.

Ultimately, acceptance of the VWfba model may lead to the development of a canopy
fire propagation model that can be related simply to LAI. This would remove the necessity
of knowing the tree species necessary to assign a SLA value. This refinement would
provide a practical method to take remotely sensed imagery and convert it directly to a
relevant canopy fuel characteristic involving one less step than the VWfba model proposed
here.

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References:


Accessed: Tuesday, April 05, 2005


Stocks BJ, Alexander ME, Wotton BM, Stefner CN, Flannigan MD, Taylor SW, Lavoie N, Mason JA, Hartley GR, Maffey ME, Dalrymple GN, Blake TW, Cruz MG, Lanoville RA


Table 1  Summary of data taken from Van Wagner (1977) used for model recalibration

<table>
<thead>
<tr>
<th>Test Fire Name</th>
<th>Fire Type</th>
<th>Basal Area (m²)</th>
<th>Trees/ha</th>
<th>Tree Height (m)</th>
<th>Height to Live (m)</th>
<th>Biomass per m²</th>
<th>CBD (kg m⁻³)</th>
<th>Actual ROS (m sec⁻¹)</th>
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<tbody>
<tr>
<td>C6 active</td>
<td></td>
<td>50</td>
<td>3200</td>
<td>14</td>
<td>7</td>
<td>1.8</td>
<td>0.23</td>
<td>0.46</td>
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<tr>
<td>C4 active</td>
<td></td>
<td>50</td>
<td>3200</td>
<td>14</td>
<td>7</td>
<td>1.8</td>
<td>0.26</td>
<td>0.28</td>
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<tr>
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<td></td>
<td>25</td>
<td>1800</td>
<td>18</td>
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</tr>
<tr>
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Table 2  Results of the equivalence test for FIA data

<table>
<thead>
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<th>FIA Data</th>
<th>n = 2626</th>
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</thead>
<tbody>
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<td>Models Compared</td>
<td>Mean of Difference (ms⁻¹)</td>
</tr>
<tr>
<td>FFE - FBA</td>
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</tr>
<tr>
<td>Cruz - FFE</td>
<td>0.050</td>
</tr>
<tr>
<td>Cruz - FBA</td>
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</table>
Figure 1  FFE methodology of canopy bulk density calculation. The maximum of the 3.97-meter (13-foot) running mean (marked with a star) read from the x-axis is the value used as the “effective CBD”.

The FFE Methodology of Canopy Bulk Density Calculation: an Example Plot with 4747 trees per hectare
Summary of Van Wagner (1977) published results and the VWfba recalibration applied to original data. Note that only the VWfba estimate is exceeded by the Actual rate of spread in the GLB fire.

*Actual = observed rate of spread; VW = Van Wagner’s published model cROS prediction; VWfba = cROS prediction for the modified model described in this paper*