.001	7.968 9.272 0.573 1.872 3.168	4.461 5.751 7.039 8.324 9.607	0.888 2.166 3.442 4.716 5.988	7.258 8.526 9.791 1.055 2.317	3.577 6.835 6.092 7.346 8.599	9.850 1.100 2.348 3.594	6.083 7.324 8.565 9.804 1.041	2.277 3.512 4.745 5.978 7.208	8.438 9.666 0.833 2.119 3.344	4.567 5.789 7.010 8.230 9.449
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0.7	43.8 45.8 45.7 45.6	2010 2010 2010 2010 2010 2010 2010 2010	56.93	57 58 59 60 61 61	664 664 664 664 664 664 664 664 664 664	67 68 70 71	72 73 17	76 77 78 79 80	81 833 854 854 854 854 854 854 854 854 854 854	10 1 80 80 80 10 10 1 1 10 10 10 10 10 10 10 10 10 10 10
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6.0	5 0 1 2 0 2 8 2 0 1 2 0 1 2 0 1 2 0 1 2 0 1 2 1 2 1 2	5 7 6 8 0 6 7 5 4 7 7 6 8 0 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	509.2 50.6 50.5 50.5 50.5 50.5 50.5 50.5 50.5	51.7 52.6 54.5 54.5 54.5 54.5 54.5 54.5 54.5 54	56.55 58 58 58 58 58 58	6 9 9 1 0 6 9 9 1 0 6 9 9 1 0	8996695 8996695	69 70 71 72 73	76	7 9 8 7 8 1 8 2 8 2
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APPENDIX 5. Tables of Critical Values for the t and Chi-square Distributions 335

Critical Values of the Chi-Square Distribution (cont.)

10		667 245 284 284	40 52 72 81	88 001 001 001	112	116 114 008	799 993 579 571	762 955 331 520	707 894 266 451
0.0		150.6 151.8 153.0 154.3 155.5	156.7 157.9 159.1 160.3 161.5	162.7 163.9 165.2 167.6	168.8 170.0 171.2 173.6	174.8 176.0 177.2 178.4 179.6	180.7 181.9 185.1 184.3 185.5	186.7 187.9 189.1 190.3 191.5	192.7 193.8 195.0 196.2
0.05		552 552 891 070	2247 2524 2754 2754 2758 2758 2758 2758 2758 2758 2758 2758	122 294 637 808	647167 641467 641467	831 11 12 12 12 12 12 12 12 12 12 12 12 12	634 957 118 278	438 597 913 070	2226 538 693 847
•	•		147 148 148 150	153. 154. 155. 157.	158. 160. 161. 162.	164 165 167 168	170. 171. 172. 174.	176. 177 178. 179. 181.	182. 183. 184. 185. 186.
10		971 154 4597 620	780 940 093 257 414	571 727 882 037 191	344 496 808 800 950	100 250 546 644	841 987 133 278 423	567 711 854 996	280 421 561 701 840
		136. 138. 140.	142. 143. 145. 146.	148. 149. 150. 153.	154. 155. 156. 153.	160. 161. 162. 162.	165. 166. 168. 169.	171 172 173 174 174	177 178 179 179 180 181
0 2	.025	700 838 975 111 247	382 517 651 784 917	049 180 311 441 571	700 829 957 084	3338 464 7164 839	962 086 331 453	575 696 816 936	175 294 412 530 648
0		131 131 132 134	136 137 138 139 140	1454	1491449	153 154 155 156	158 160 161 162 163	164 165 165 167 167	170 171 172 173
0	0,05	.458 .574 .689 .804 .918	031 144 257 369	591 701 811 921 030	.138 .3546 .461	. 674 . 779 . 885 . 989 . 094	198 302 405 508 610	712 814 915 016	216 316 415 514 613
0		125 126 127 128 128	131 132 133 134 135	136 137 138 138 159 141	65432 14444 15111	147 148 149 150 152	153 154 155 155	1538 1630 1631 1631	164 165 166 167
	.10	589 679 769 858	035 123 211 298 385	472 558 543 729 813	898 982 066 149	315 398 480 562	724 805 9655	125 204 283 561 561	7.518 8.595 9.673 0.750 1.827
0		119 120 122 123	125 126 127 127 128	134	135		3 146 6 147 8 148 0 149 2 151	4 152 6 153 8 154 9 1554 0 156	4 1 1 2 8 3 1 2 3 4 1 2 3 8 3 1 2 3 4 1 2 3 8 3 1 2 3 8 3 1 2 3 8 3 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 2 3 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
- 7	. 25	236 236 284 284	5.424 6.471 7.517 8.563 9.608	0.654 1.699 2.744 3.784 4.834	5.878 6.923 7.967 9.011 0.055	1.098 2.142 5.185 5.271 5.271	6.313 8.356 9.440 0.482	00000 0000 0000 0000 0000	6 731 8 813 9 854
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· ·	0.75	4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	5.85 6.80 7.75 8.71 9.66	6	5.39 6.35 7.30 8.26	0.17 1.13 2.08 3.04	4 95 5 91 8 79 8 79	19,75 20,70 21,66 22,62 23,58	8.38 8.38 8.38 8.38 8.38 8.38 8.38 8.38
		000000		20102 20102 20102	58 10 74 10 90 10 24 10	41 11 58 11 76 11 13 13		52 11 52 12 17 12 12 12 12	38 12 61 12 83 12 06 12 29 12
06 0		13.26 14.17 15.999 15.999	87.82 88.73 89.64 90.55 91.47	92.38 93.29 94.21 95.12 96.04	96.95 97.87 98.79 99.70 00.62	01.54 02.45 04.25 04.25	07.05 07.05 08.80 09.81 09.81	110.73	15.33 16.26 18.10
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ribution 0.975		273 273 273 273 273 273 273 273 273 273	00 60 61 61	177450 177400	88 20 20 20 20 20 20 20 20 20 20 20 20 20	46 20 46 1	22 1 98 1 53 1 1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2	101 830 48 18 10 10 10 10 10 10 10 10 10 10 10 10 10	009 1 91 1 54 1 37 1
istrib 0.9	۶.	75.0 75.9 776.8 77.6	79.4 80.2 81.1 82.8 82.8	85.5 85.5 85.5 87.3	888 888 9 9 9 9 7 9 7 9 1 9 1 9 1 9 1 9 1 9 1 1 9 1 1 9 1	92,49 94,13 95,00 95,90	96.56 98.55 99.45 99.45 99.45	01.02	105.6 107.3 109.1
De P		22	58 58 58	82 81 10 10 10 10 10 10 10 10 10 10 10 10 10	229	77 624 524 3225 180	033 887 741 451 1	307 1 163 1 021 1 878 1 736 1	1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
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Chi-S	•	140 965 785 428 428	251 251 225 250 250	377 204 862 692	522 353 0185 852	686 521 356 029	866 3845 2845 2845	063 904 588 431	275 119 964 809 655
Critical Values of the Chi-Square Dist	•	688 70.00 71.00	25232	91886	2010 2010 2010 2010 2010 2010 2010 2010	888888 84075	8 8 5 5 5 5 8 7 0 1 N	000000 000000	200 80 80 80 80 80 80 80 80 80 80 80 80 8
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MEASURING AND MONITORING PLANT POPULATIONS

Statistical Tables and Graphs

Table B.1 was prepared using Equation 26.4.6 of Zelen and Severo (1964). The chi-square values were calculated to six decimal places and then rounded to three decimal places.

Examples:

$$\chi^2_{0.05,12} = 21.026$$
 and $\chi^2_{0.0,138} = 61.162$

For large degrees of freedom (v), critical values of χ^2 can be approximated very well by

$$\chi^{2}_{\alpha,\nu} \simeq \nu \left(1 - \frac{2}{9\nu} + Z_{\alpha(1)} \sqrt{\frac{2}{9\nu}}\right)^{3}$$

(Wilson and Hilferty, 1931). It is for this purpose that the values of $Z\alpha(1)$ are given below (from White, 1970).

	$\alpha = 0.999$		0	.995	0.99		0.975			0.95		0.90		0.75		
	$Z_{\alpha(1)} = -3.09023$		-2.	57583	-2.32635		-1.95990		96	6 -1.64485		-1.28155		-0.67449		
	$\alpha = 0.50$		0	0.25 0.10		0.05		0.02	0.025 0.01		0.005		0.001			
	$Z_{\alpha(1)}=0.00000$		0.6	7449	1.28155		1.644	54485 1.9599		96	6 2.32635		5 2.57583		3.09023	
	The percent error, i.e., (approximation – true value)/true value \times 100%, resulting from the use of this approximation is as follows:													use of		
V	a = 0.999	0.995	0.99	0.975	0.95	0.90	0.75	0.50	0.25	0.10	0.05	0.025	0.01	0.005	0.001	
30 100 140	-0.7 -0.1 0.0*	-0.3 0.0* 0.0*	-0.2 0.0* 0.0*	-0.1 0.0* 0.0*	0.0* 0.0* 0.0*	0.1 0.0* 0.0*	0.2 0.0* 0.0*									

where the asterisk indicates a percent error the absolute value of which is less than 0.05%. Zar (1978) discusses this and other approximations for $\chi^2_{\alpha,\nu}$.

For one degree of freedom, the χ^2 distribution is related to the normal distribution (Appendix Table B.2) and the t distribution (Appendix Table B.3) as

$$\chi^2_{\alpha,1} = \left(Z_{\alpha(2)} \right)^2 = \left(t_{\alpha(2),\infty} \right)^2$$

For example, $\chi^2_{0.05,1} = 3.841$, and $(Z_{0.05(2)})^2 = (t_{0.05(2),\infty})^2 = (1.9600)^2 = 3.8416$. The relationship between χ^2 and F (Appendix Table B.4) is

$$\chi^2_{\alpha,\nu}=\nu F_{\alpha(1),\nu,\infty}.$$

For example, $\chi^2_{0.05,9} = 16.919$, and $(9)(F_{0.05(1),9,\infty}) = (9)(1.88) = 16.92$.